

# Local cues and global constraints in image understanding



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\*Many slides adopted from the courses of Anton Konushin

# Image understanding



- «To see means to know what is where by looking»  
– *David Marr, Vision, 1982*



0	3	2	5	4	7	6	9	8
3	0	1	2	3	4	5	6	7
2	1	0	3	2	5	4	7	6
5	2	3	0	1	2	3	4	5
4	3	2	1	0	3	2	5	4
7	4	5	2	3	0	1	2	3
6	5	4	3	2	1	0	3	2
9	6	7	4	5	2	3	0	1
8	7	6	5	4	3	2	1	0

We see

Computer sees

Slide credit S. Narasimhan



## • Scene interpretation

- outdoors
- urban
- street
- Beijing, China



- Object detection



- Extracting details about the objects

Blue

Inclined

Moving

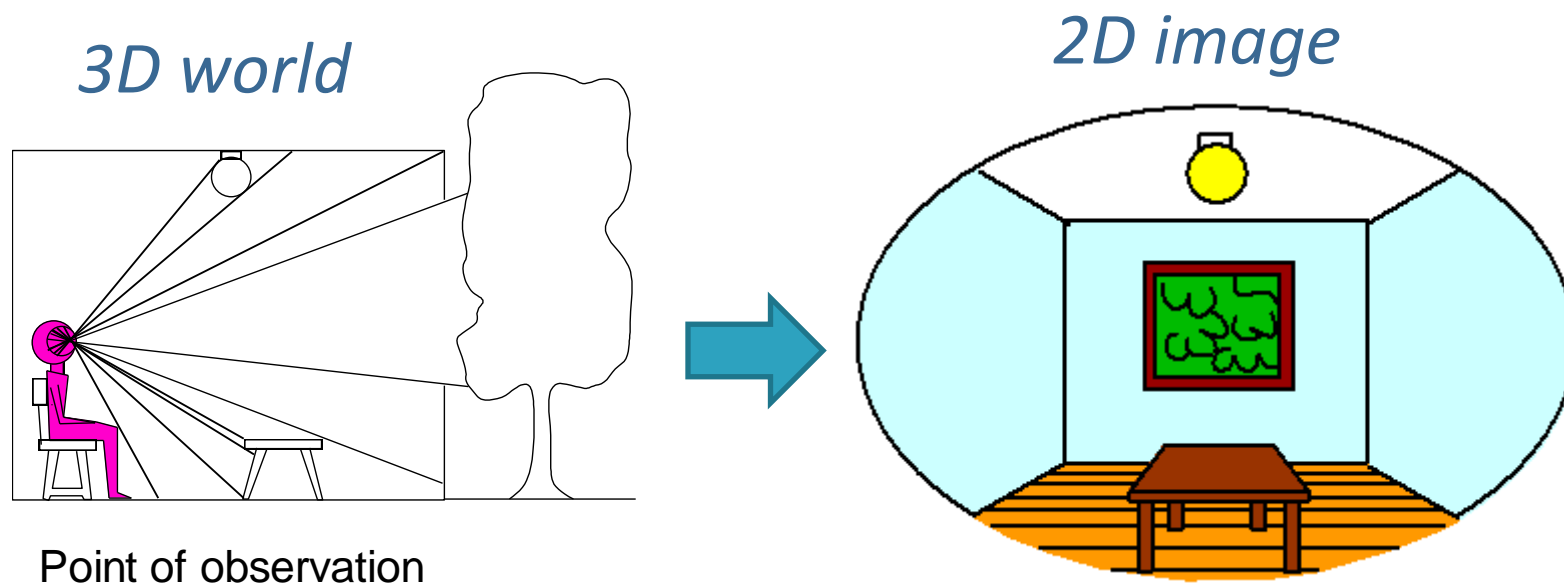
Mao

Moving



# Why is image understanding difficult?

- Dimensionality reduction



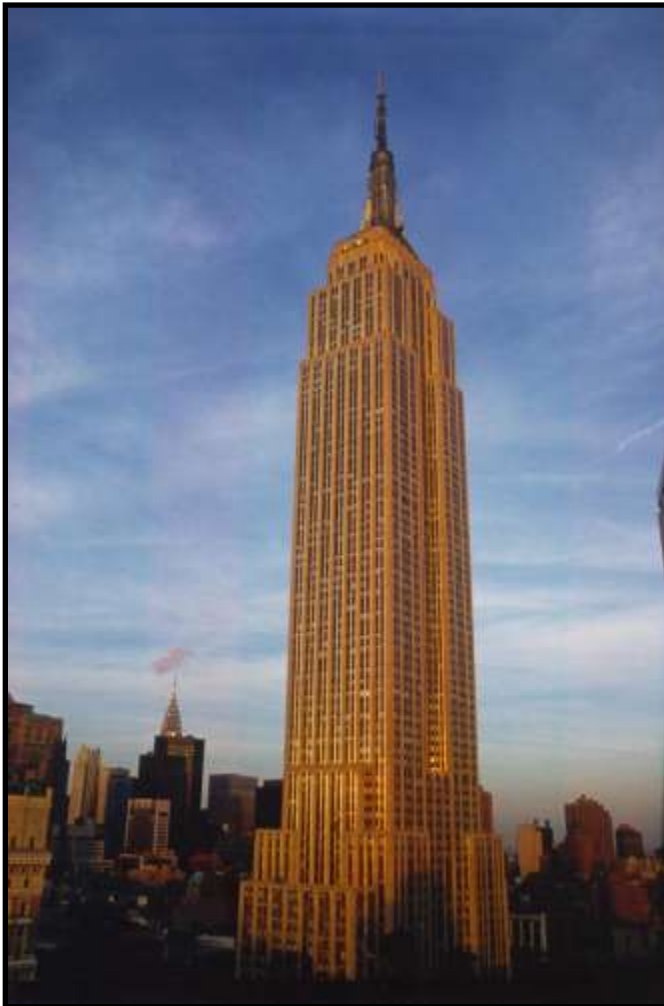
## What do we lose in perspective projection?

- Angles
- Distances and lengths

Figures © Stephen E. Palmer, 2002

# Why is image understanding difficult?

- Variability: interclass variability of appearance





# Why is image understanding difficult?

- Variability: different viewpoints



Michelangelo 1475-1564



slide credit: Fei-Fei, Fergus & Torralba

# Why is image understanding difficult?

- Variability: different lighting

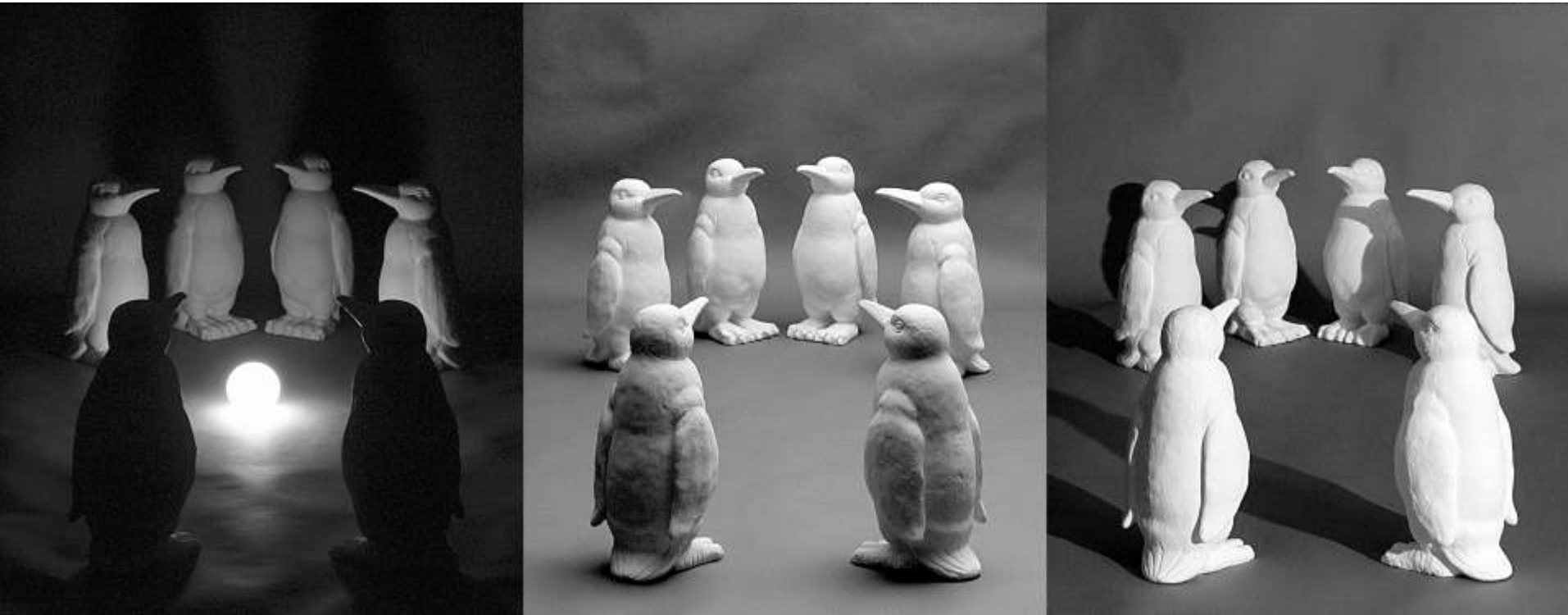
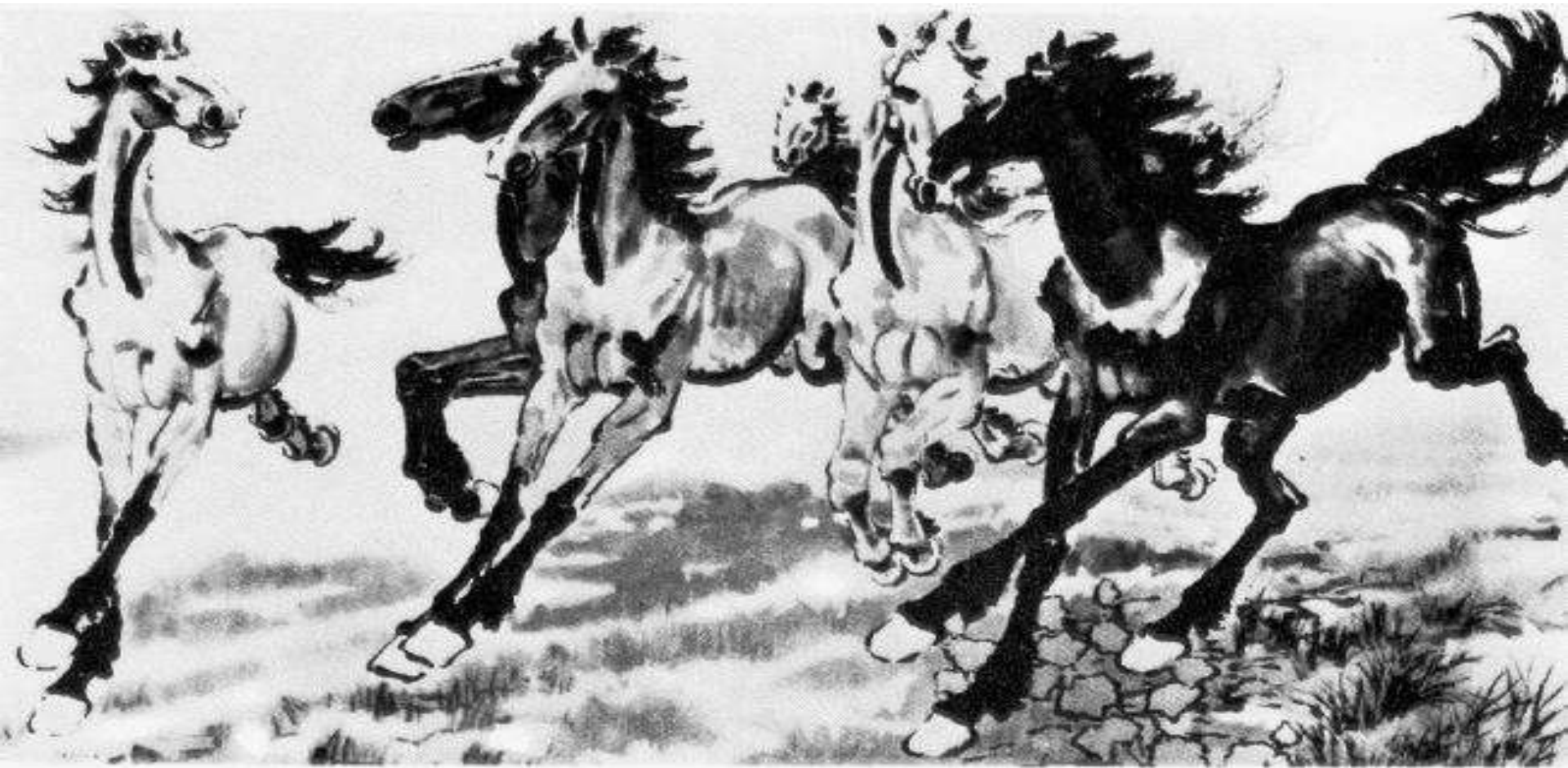


image credit: J. Koenderink

# Why is image understanding difficult?

- Variability: deformations and occlusions



Xu, Beihong 1943

Slide credit: Fei-Fei, Fergus & Torralba

# Reducing variability by using local cues

- Motivation: stitching panoramas
  - Find distinctive points
  - Find an alignment that matches these points



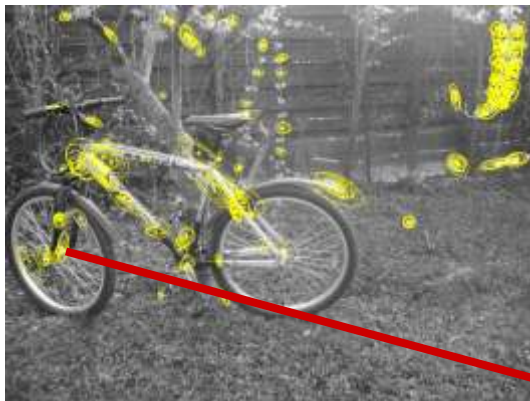
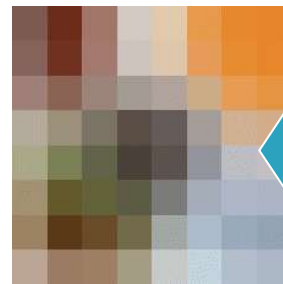
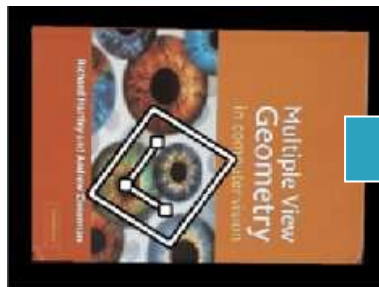
# Reducing variability by using local cues

- Motivation: stereo matching



# Reducing variability by using local cues

- Motivation: image retrieval object detection

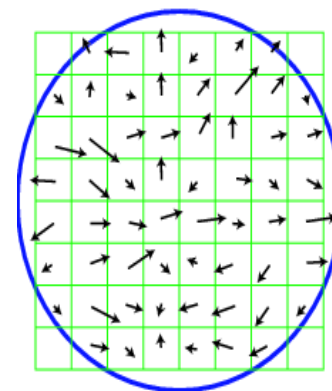
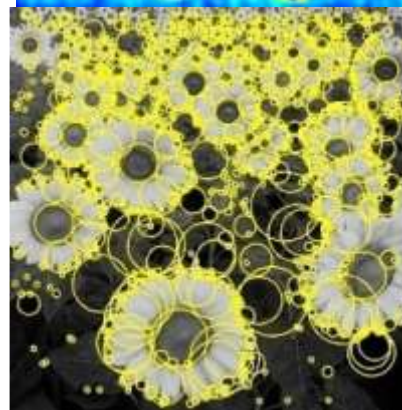
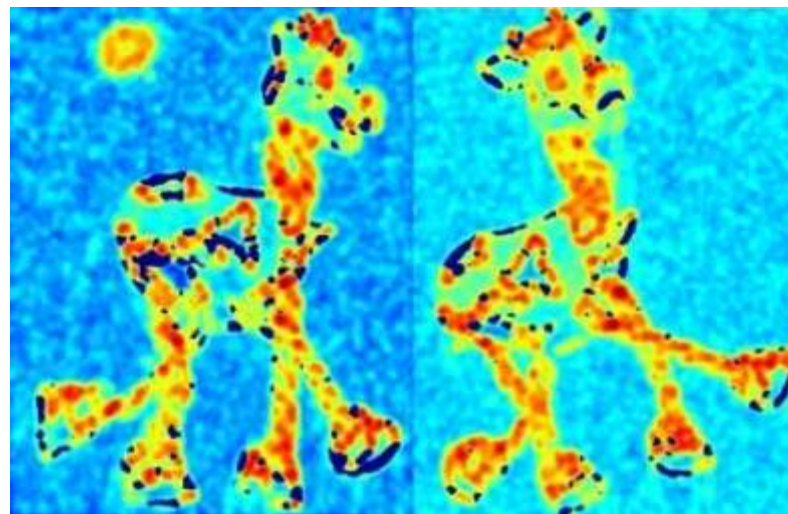


Slide credit: S. Lazebnik

# Learning local models from local cues

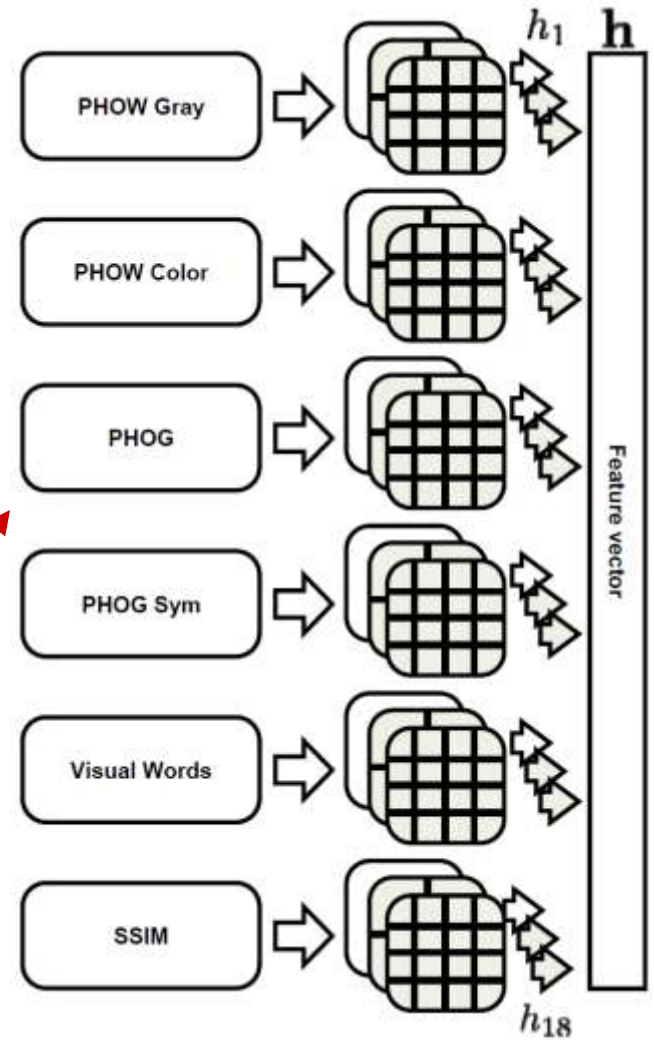
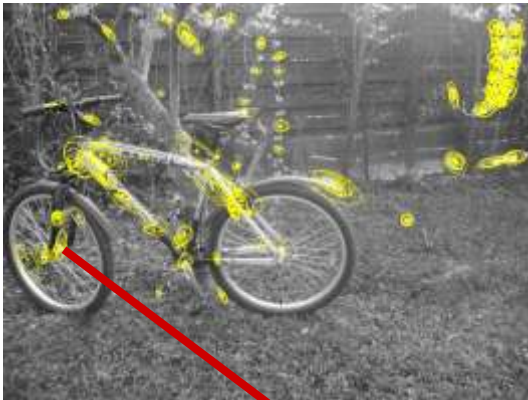
## • Local features and descriptors

- Feature detectors
  - Harris-Laplace
  - LoG
  - DoG
  - Dense sampling
- Descriptors
  - SIFT
  - Shape context
  - HOG
  - Pixel comparison



# Learning local models from local cues

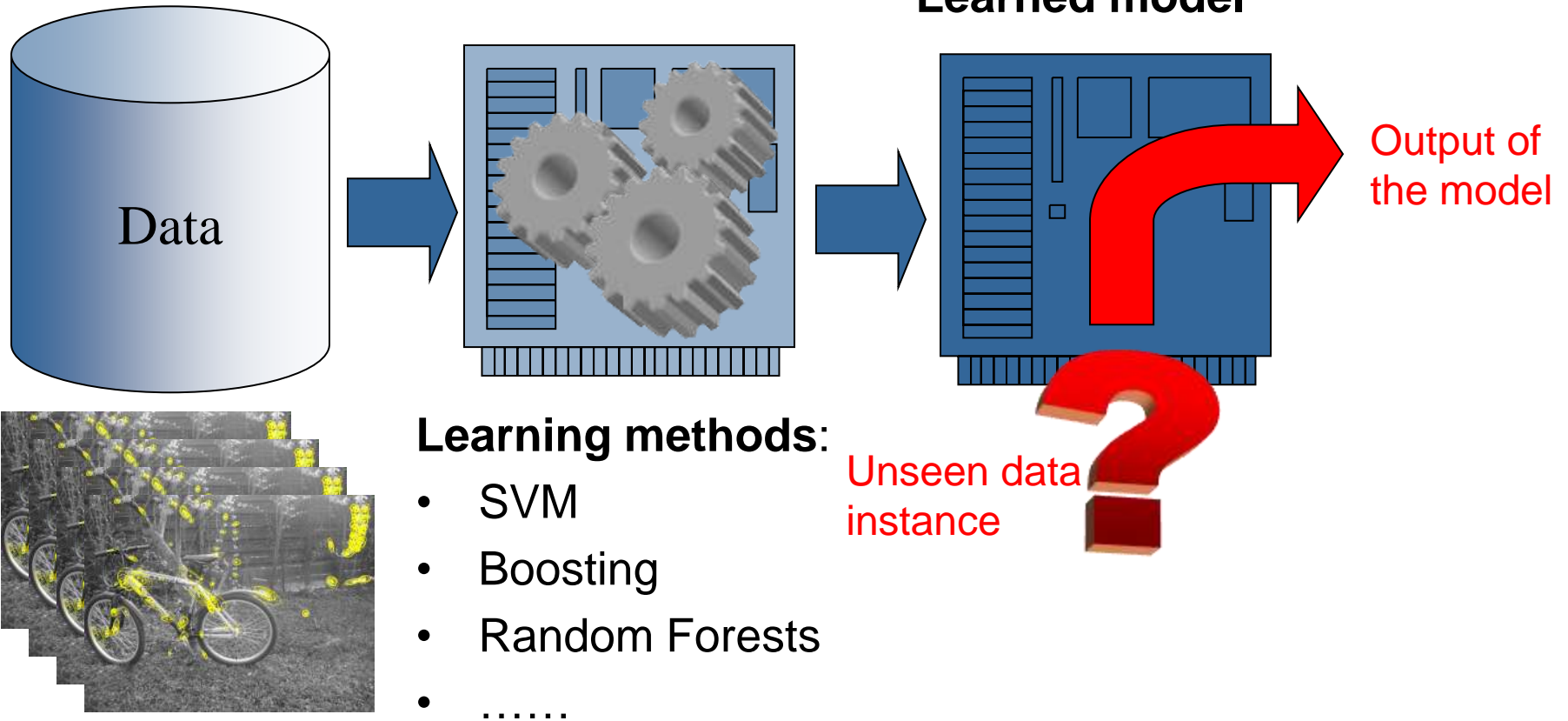
- Combining different descriptors





# Learning local models from local cues

- Learning models from the data



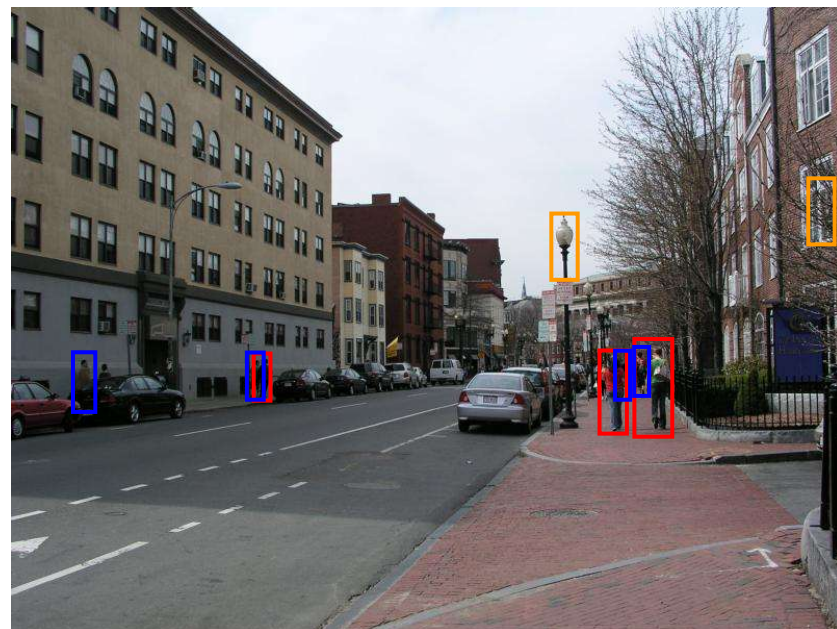
# Learning local models from local cues

## • Example: object detection using sliding window

- 'Local' has been the dominant paradigm in computer vision till the 2000s
- Works notoriously well for detection of rigid objects, e. g. faces

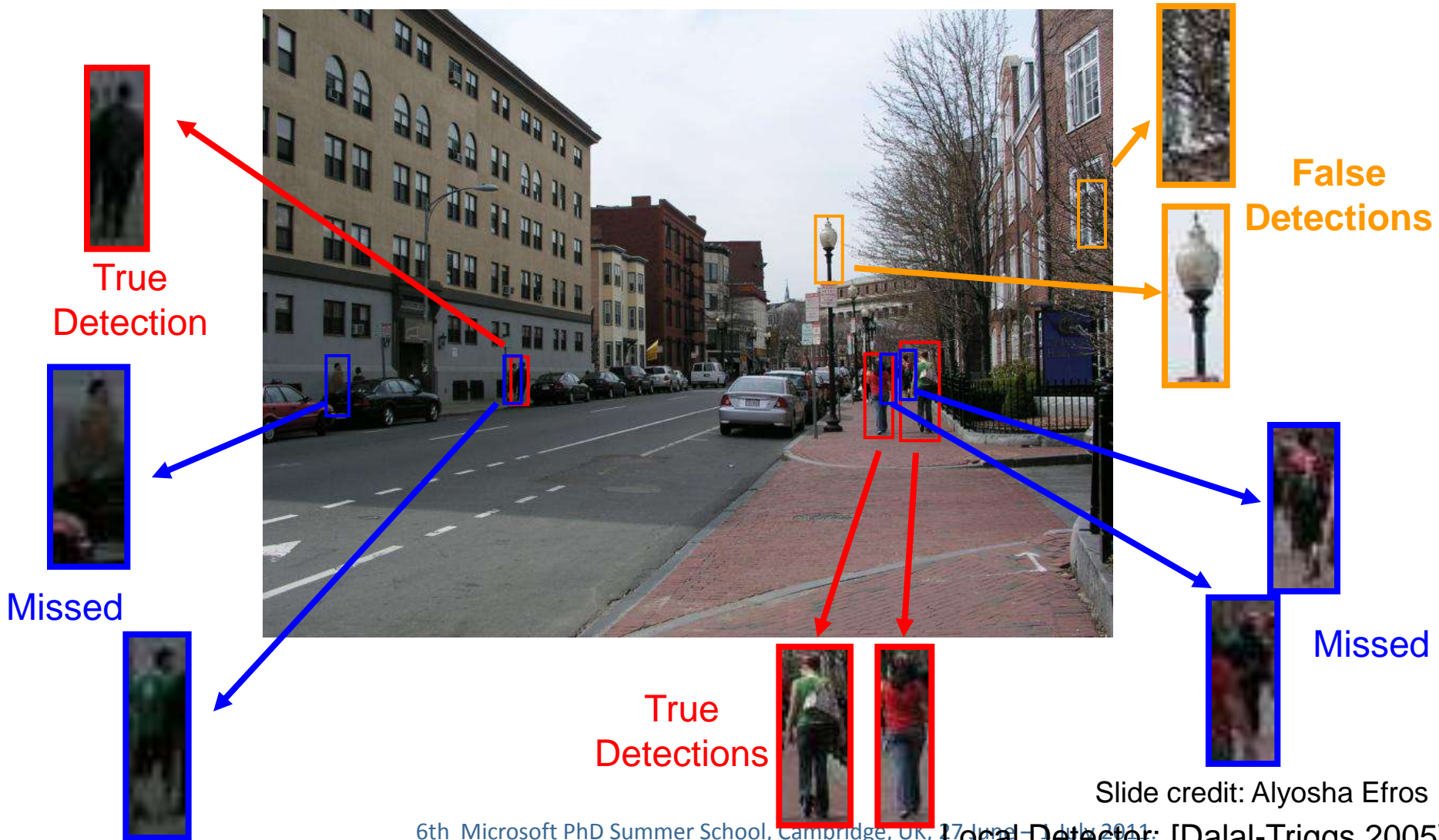
[Viola, Jones, 2001],

[Dalal, Triggs, 2005]



# Learning local models from local cues

- Let's have a closer look at the results



Slide credit: Alyosha Efros

# Learning local models from local cues

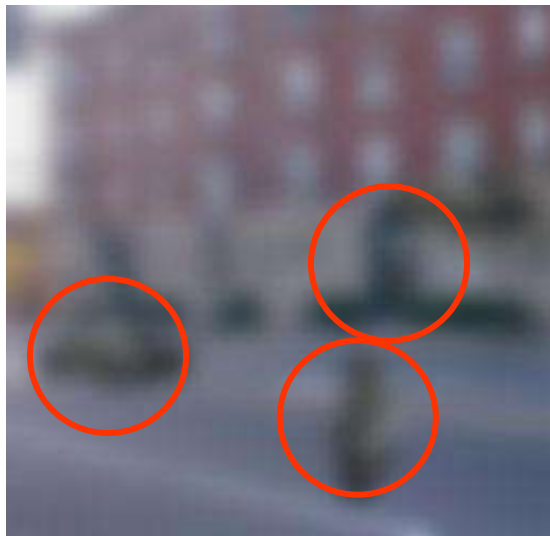
- What the detector sees



Slide credit: Alyosha Efros

# Learning local models from local cues

- Local ambiguity



Slide credit: Fei-Fei, Fergus & Torralba

# Learning local models from local cues

- The role of context



Slide credit: Fei-Fei, Fergus & Torralba

# Learning local models from local cues

- The role of context



Slide credit: Fei-Fei, Fergus & Torralba

# Constraints of the world

- The world is structured, not everything is possible

- Local cues
  - Similar appearance of similar objects
- Global constraints
  - Limited number of allowed deformations of the objects in 3d
  - Depth ordering and occlusions
  - Rules of perspective projection
  - ....



Chaotic world



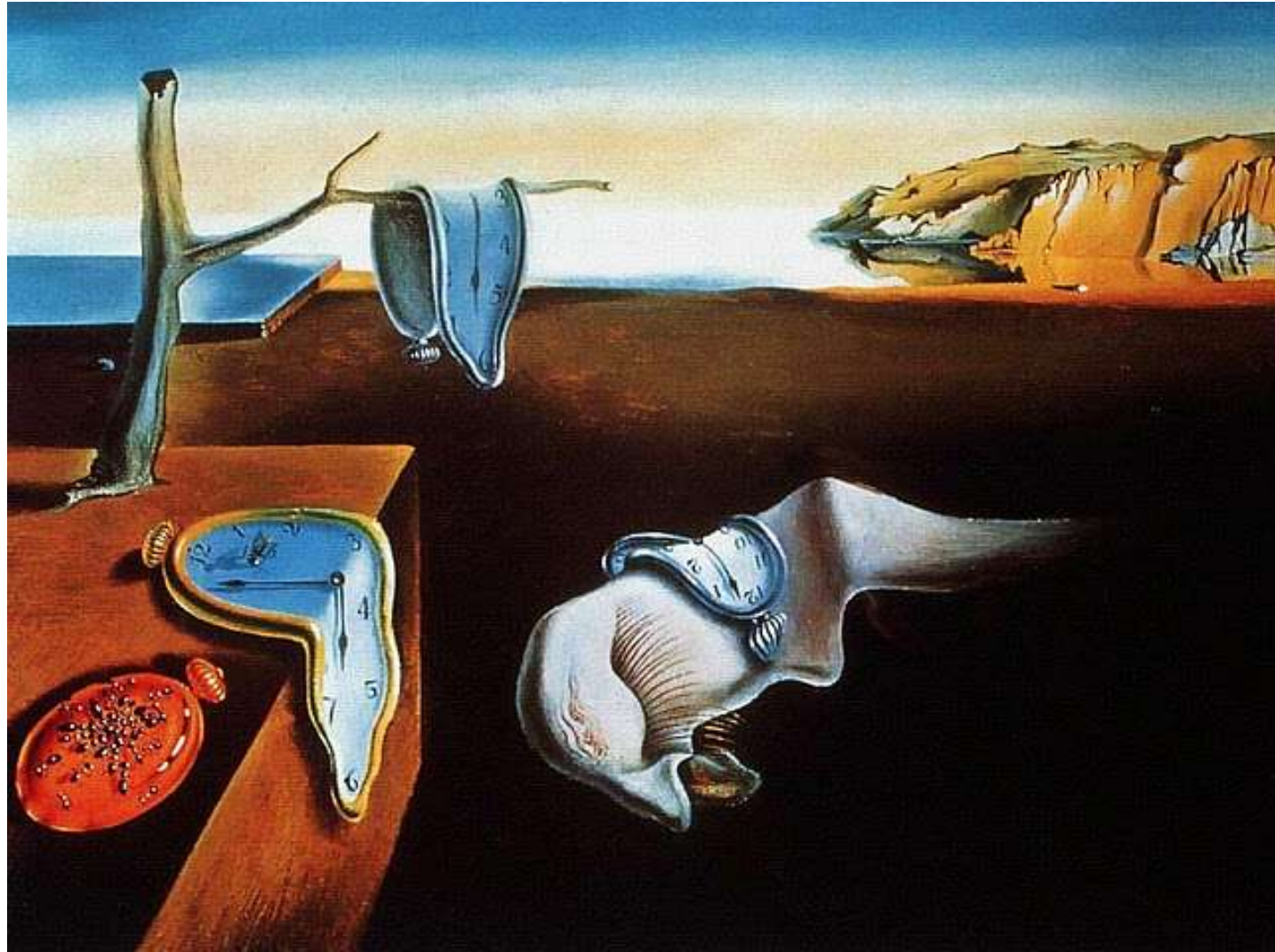
Structured world



# Constraints of the world

- Limited set of allowed deformations for the objects

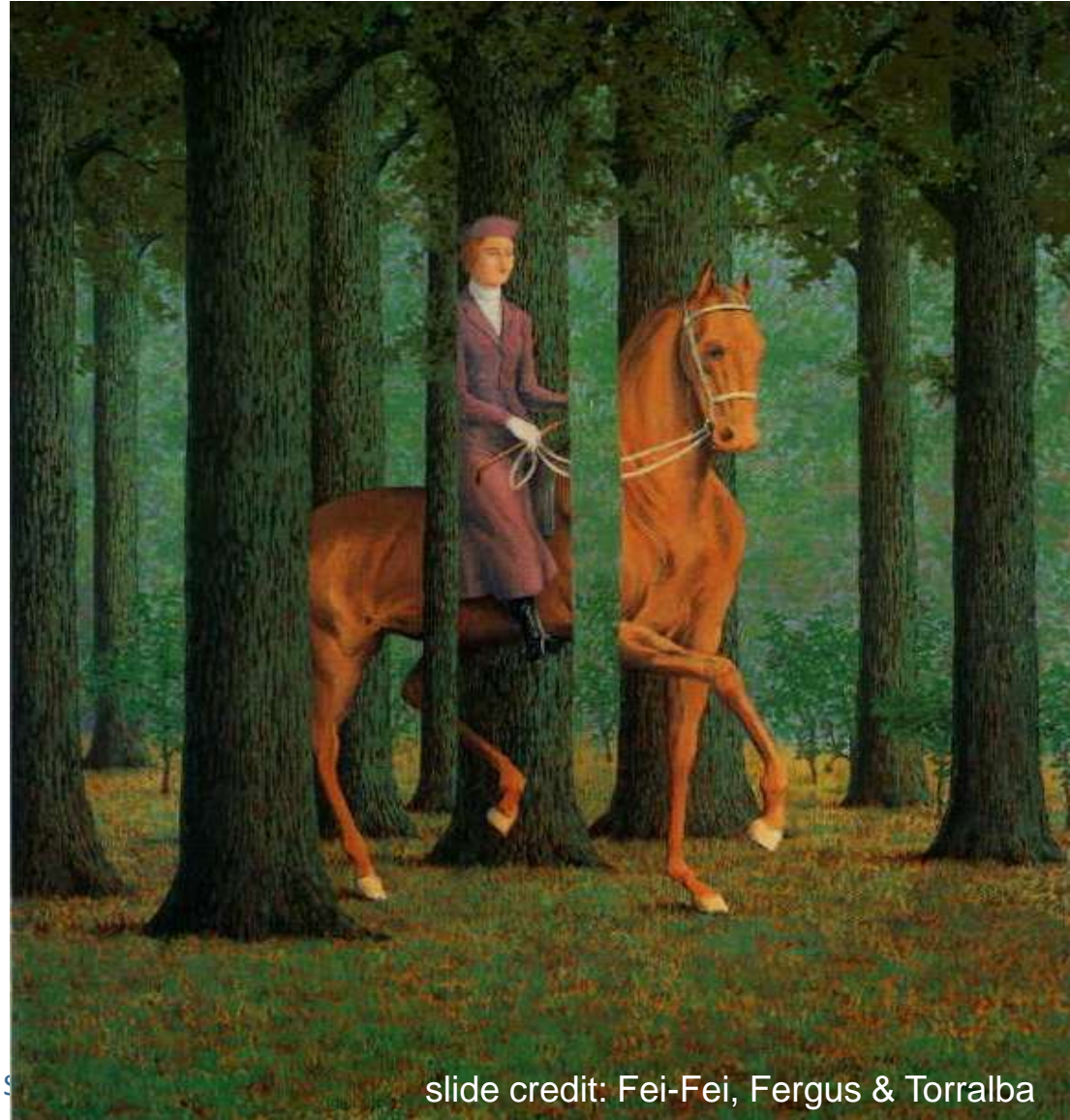
Dali, 1931



# Constraints of the world

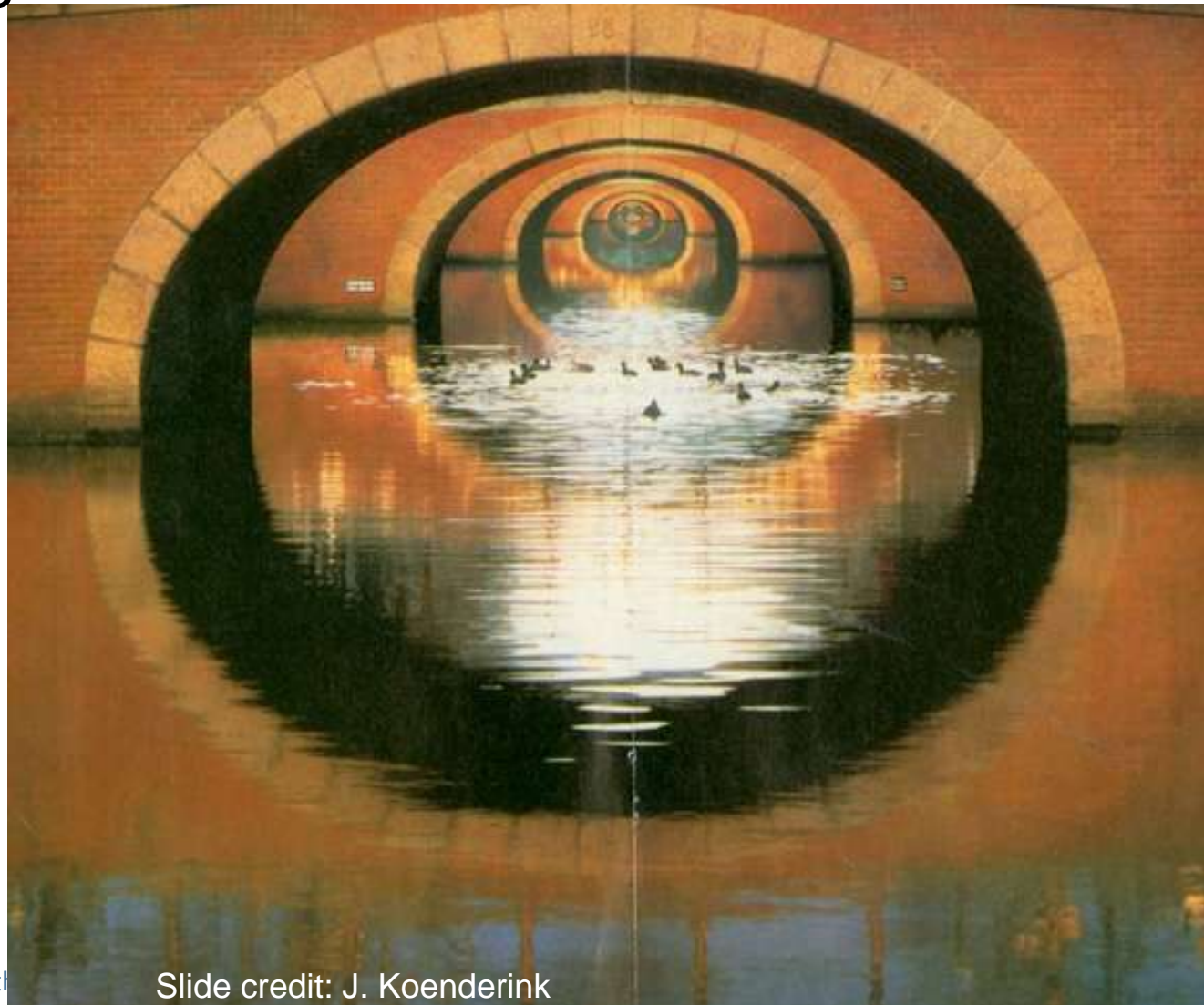
- Occlusions

Magritte, 1957



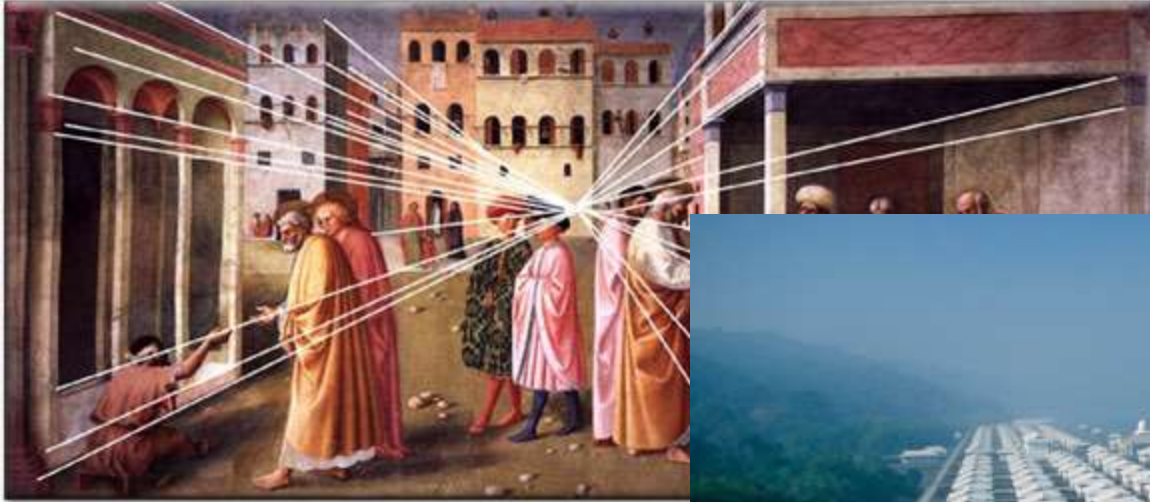
# Constraints of the world

- Depth ordering

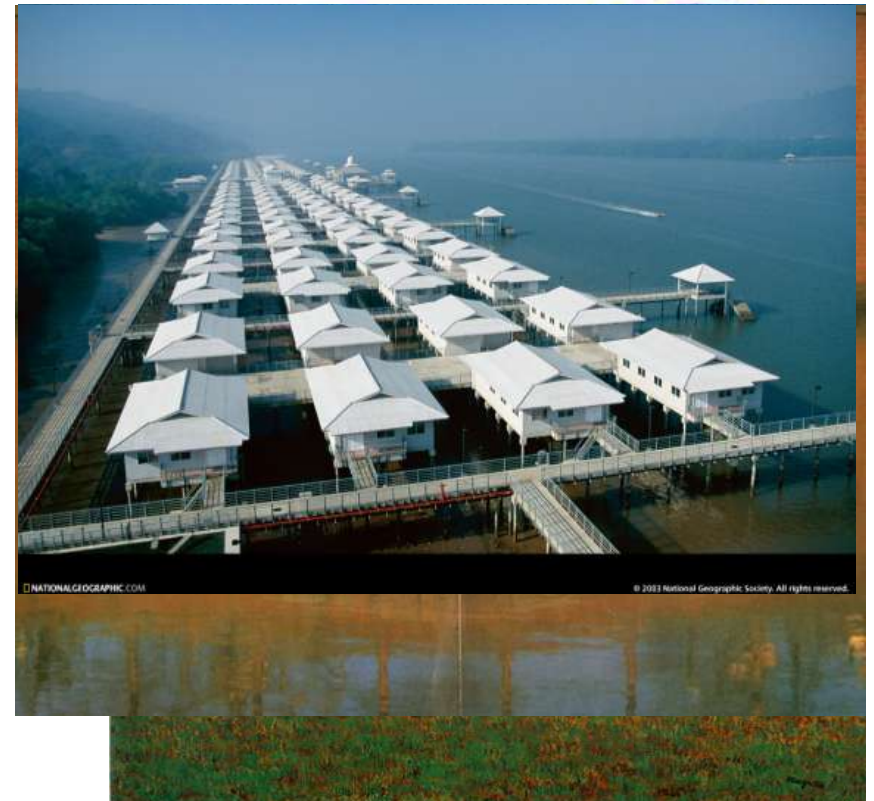


# Constraints of the world

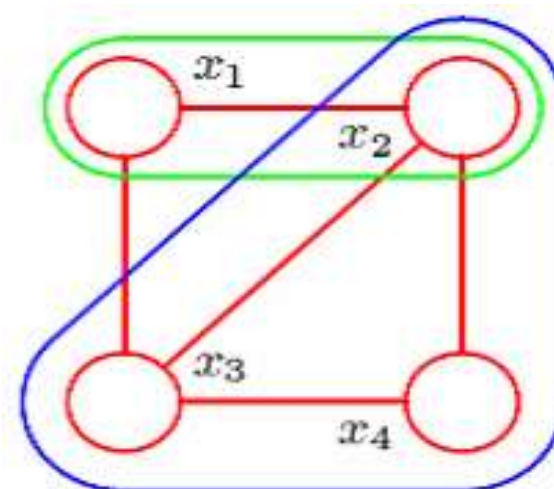
- Rules of perspective geometry



- Outline of the talk
  - The idea of graphical models
  - Examples:
    - Limiting the set of allowed deformations
    - Occlusion constraint
    - Depth ordering constraint
    - Modeling the rules of perspective geometry

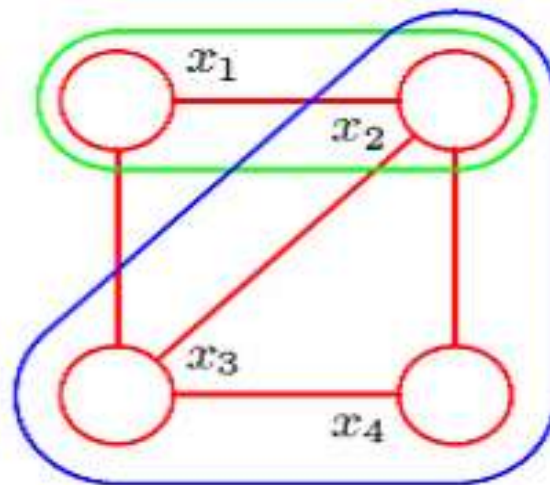


- Outline of the talk
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- Graphical models

- Graphical representation of probability distributions
- Graph-based algorithms for calculation and computation
- Capture both local cues and global constraints by modeling dependencies between random variables

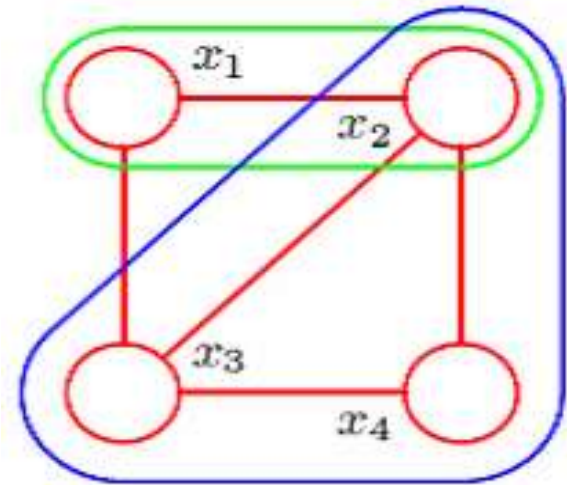


Picture credit: C. Bishop

# Graphical models

- Graph representation

- Each node corresponds to a **random variable**
- **Dependent variables** are connected with edges



- **Clique** - fully connected set of nodes in the graph
- **Maximal clique** - a clique that is not a subset of any other cliques

$$p(x_1, x_4 / x_2, x_3) = p(x_1 / x_2, x_3) p(x_4 / x_2, x_3)$$

Picture credit: C. Bishop



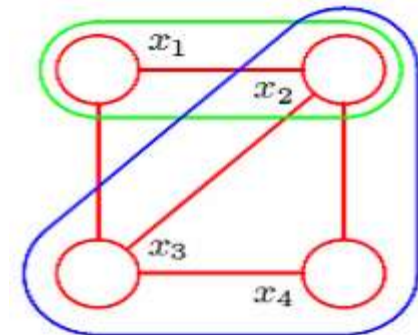
# Graphical models

- Joint distribution and potentials

Joint distribution of all random variables can be written as a product of nonnegative **potentials** defined on maximal cliques:

$$p(X) = \frac{1}{Z} \prod_C \psi_C(X_C) \quad Z = \sum_X \prod_C \psi_C(X_C), \quad \psi_C(X_C) \geq 0$$

$$p(X) = \frac{1}{Z} \psi_1(x_1, x_2, x_3) \psi_2(x_2, x_3, x_4)$$

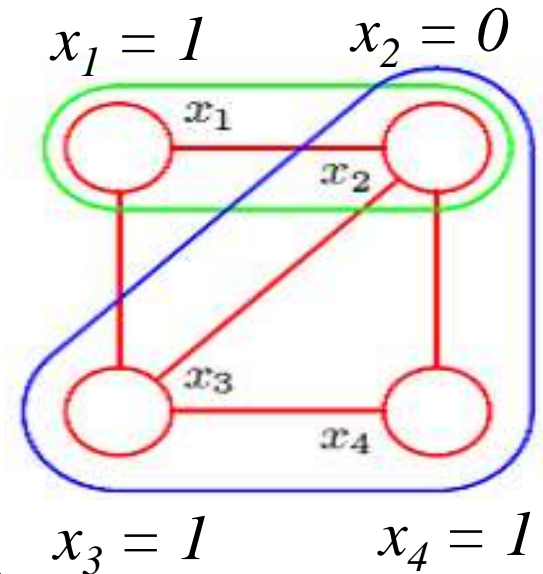


# Graphical models

- MAP-inference and energy function

**Maximum a-posteriori (MAP) inference** - find the values of all variables in the graphical model that maximize the joint probability

$$\begin{aligned} \arg \max p(X) &= \arg \max \frac{1}{Z} \prod_c \psi_c(X_c) = \\ &= \arg \max \exp\left(-\sum_c E_c(X_c)\right) = \\ &= \arg \min \sum_c E_c(X_c) \end{aligned}$$



**Energy function:**  $E(X) = \log P(x) = \sum_c E_c(X_c)$

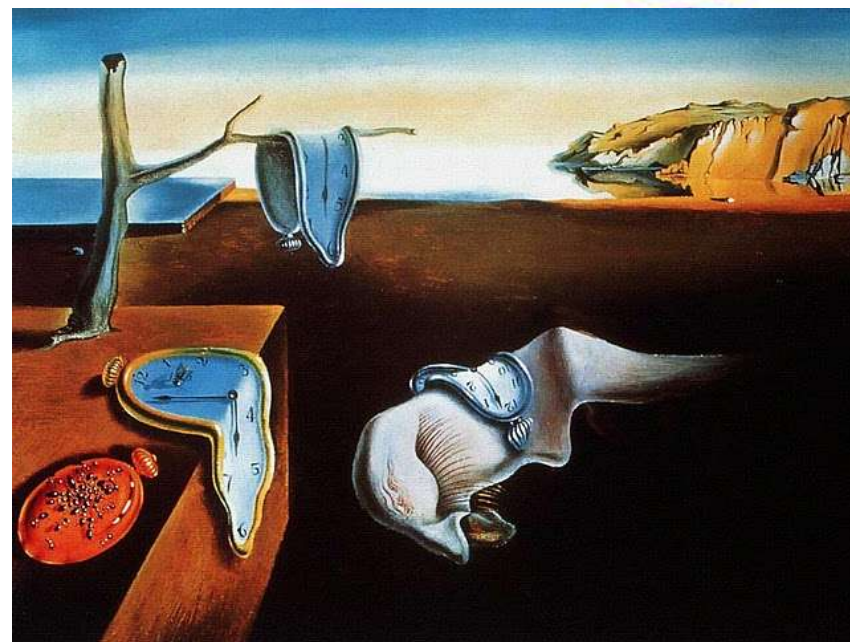
**MAP-inference = energy minimization**

# Graphical models

- Methods for MAP-inference
  - Many computationally efficient methods for inference in graphical models have been developed:
    - graph cuts
    - TRW
    - belief propagation
    - expectation propagation
    - MCMC
    - ....
  - All these methods have limitations and can be used to minimize energy functions of specific forms → the art is to find tradeoff between flexibility and tractability

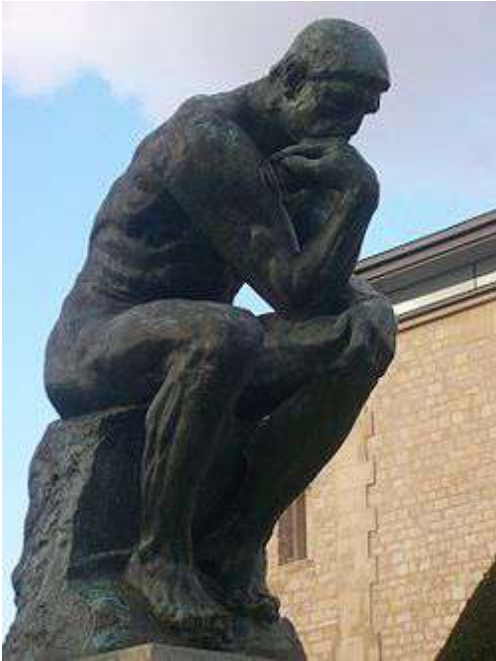
- Outline of the talk

- The idea of graphical models
- **Examples:**
  - **Limiting the set of allowed deformations**
  - Occlusion constraint
  - Depth ordering constraint
  - Modeling the rules of perspective geometry



# Expressing constraints with graphical models

- Limiting the set of allowed deformations



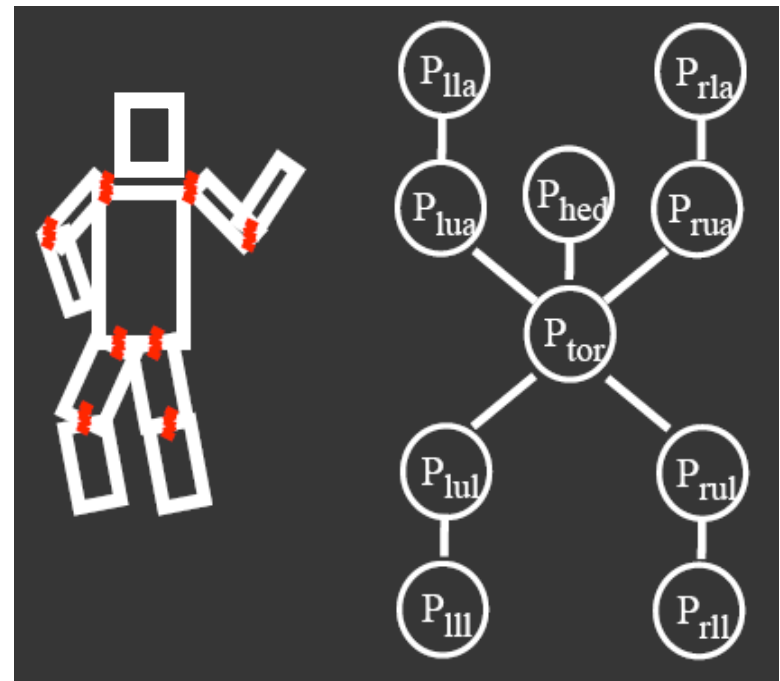
- Model should be flexible enough, but constrain the allowed deformations of an object

# Limiting the set of allowed deformations

- Pictorial structures model

- **Pictorial structures** strike a good balance between flexibility and tractability

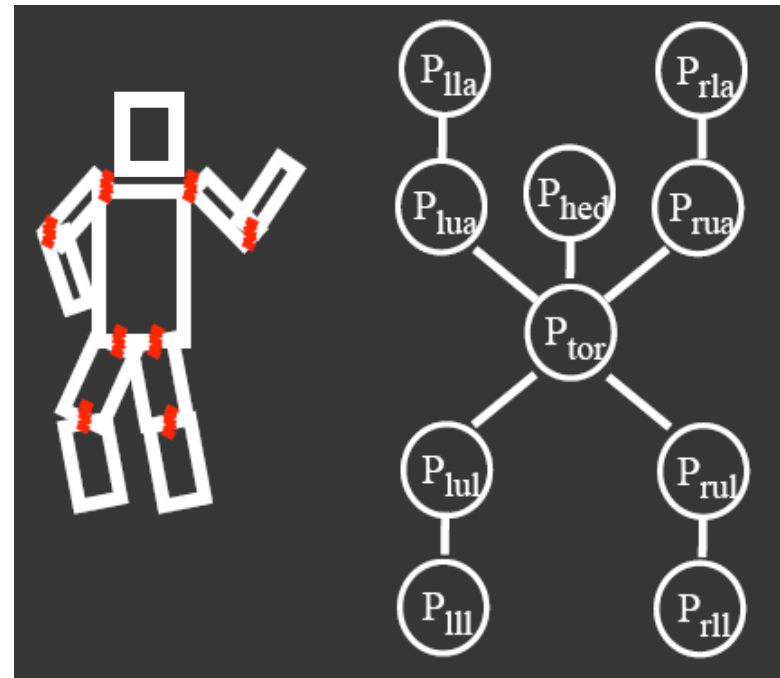
[Fischler & Elschlager 73],  
[Felzenszwalb & Huttenlocher 00]



# Limiting the set of allowed deformations

- Pictorial structures model

- Each vertex corresponds to a part of a person: *'Head'*, *'Torso'*, *'Legs'*, *'Arms'*
- Edges form a tree
- Person detector - for each vertex find a corresponding position from the set of valid positions



$$\Pr(P_{\text{tor}}, P_{\text{arm}}, \dots | \text{Im}) \propto \prod_{i,j} \Pr(P_i | P_j) \prod_i \Pr(\text{Im}(P_i))$$

↑
↙  
 part geometry                      part appearance

# Limiting the set of allowed deformations

- Pose estimation



- Pedestrian detection

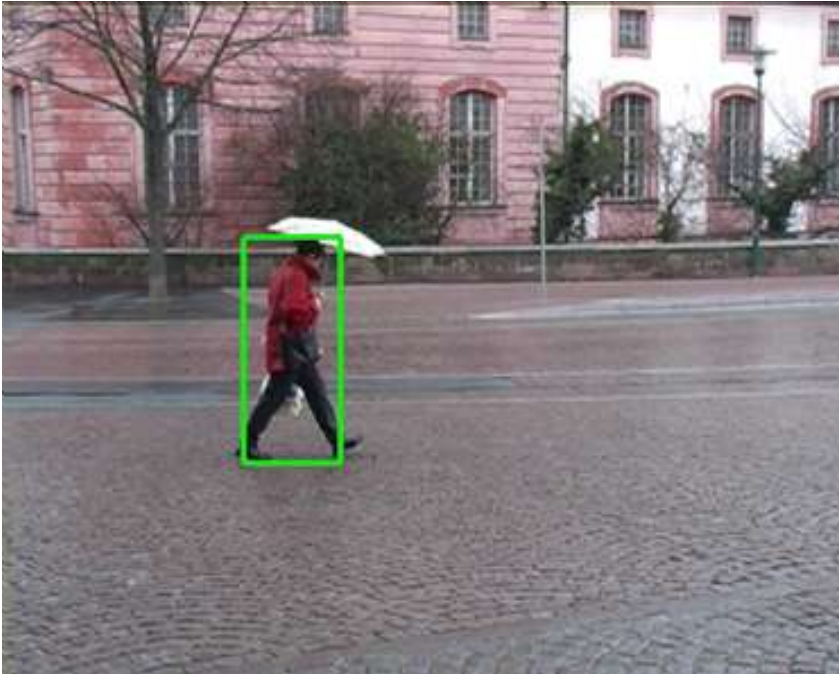




- Outline of the talk
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- Occlusions

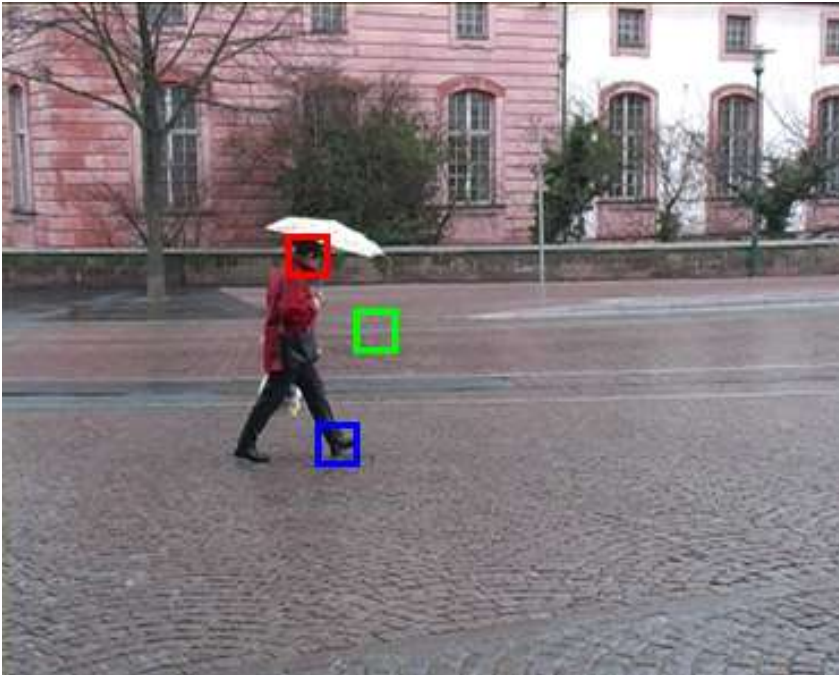


- Occlusions and self occlusions make the task of object detection even harder

Joint work with Victor Lempitsky and Pushmeet Kohli, CVPR10

# Occlusion constraint

- Local model

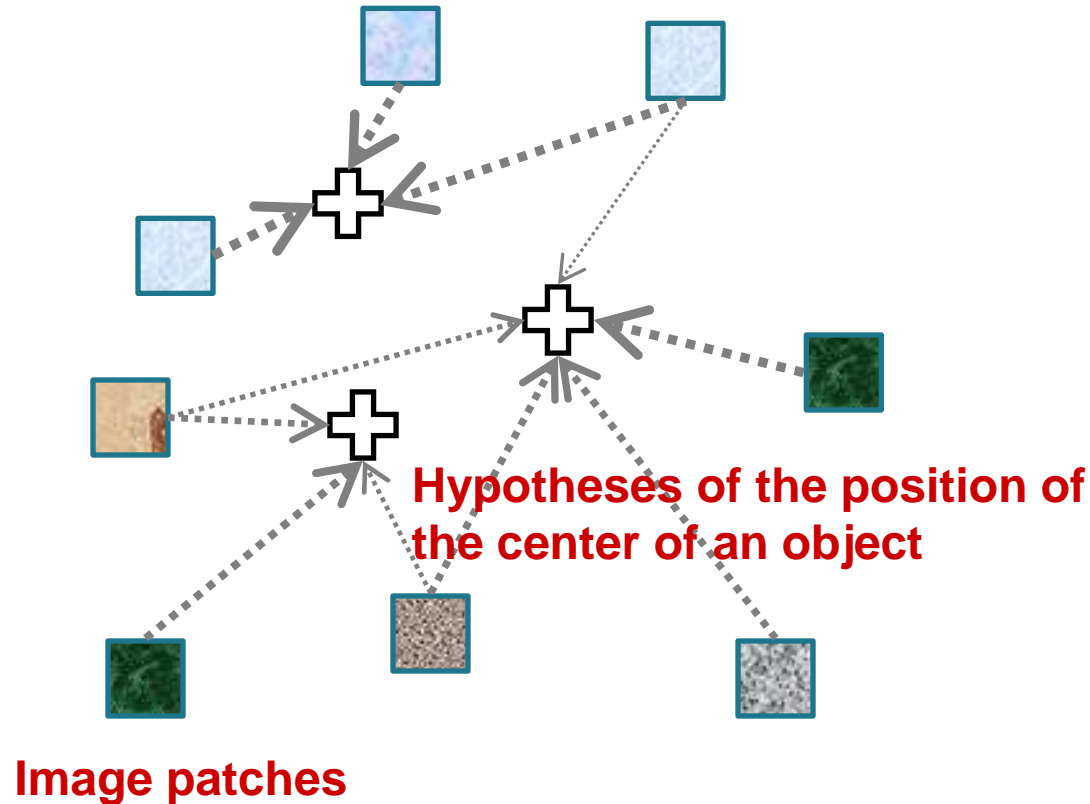


Model from [Gall & Lempitsky, CVPR09]

Joint work with Victor Lempitsky and Pushmeet Kohli, CVPR10

# Occlusion constraint

- Each image pixel belong to no at most one object

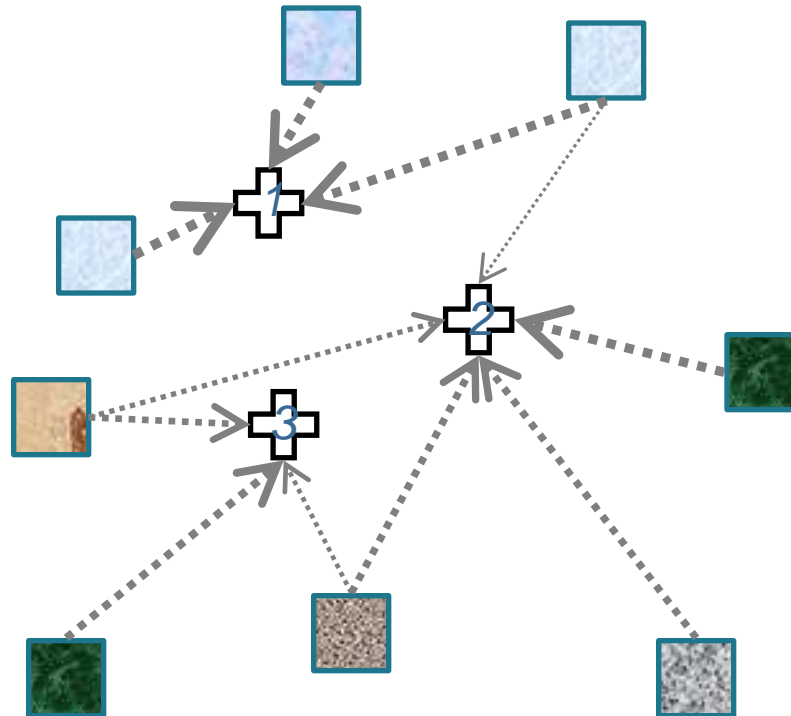


Joint work with Victor Lempitsky and Pushmeet Kohli, CVPR10

# Occlusion constraint

- Modeling the occlusion constraint

$x$  – labelling of image patches,  
 $x_i = 1$ , if the patch votes for hypothesis,  
 $x_i = 0$ , if the patch votes for background



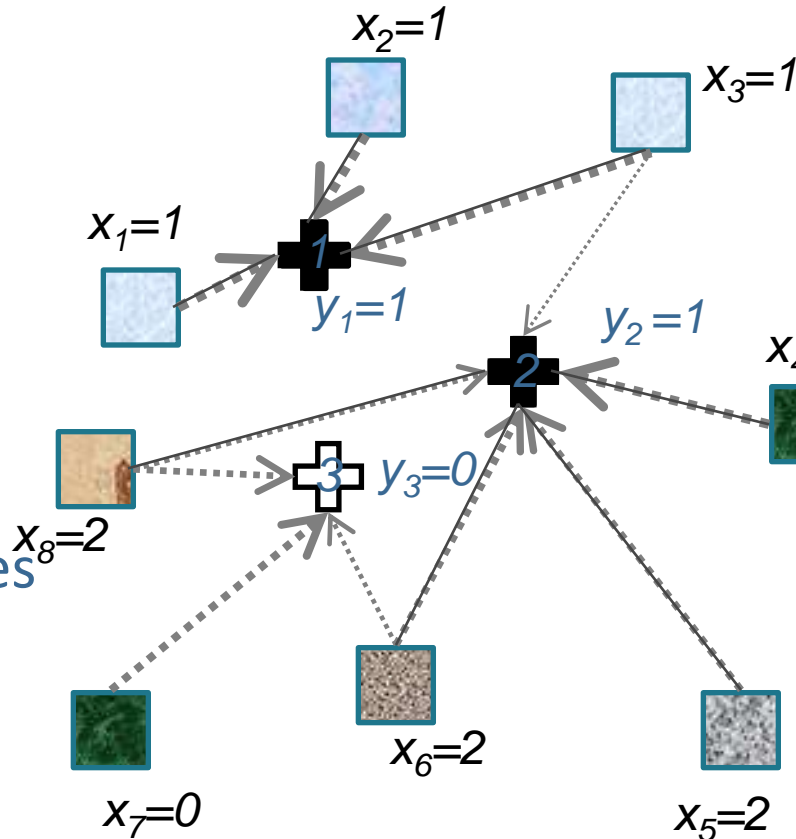
$y$  – labelling of hypotheses,  
 binary variables:  
 $y = 1$ , if the object is present,  
 $y = 0$ , otherwise

Joint work with Victor Lempitsky and Pushmeet Kohli, CVPR10

# Occlusion constraint

- Modeling the occlusion constraint

$x$  – labelling of image patches,  
 $x_i = \text{index of hypothesis, if the patch votes for hypothesis,}$   
 $x_i = 0$ , if the patch votes for background



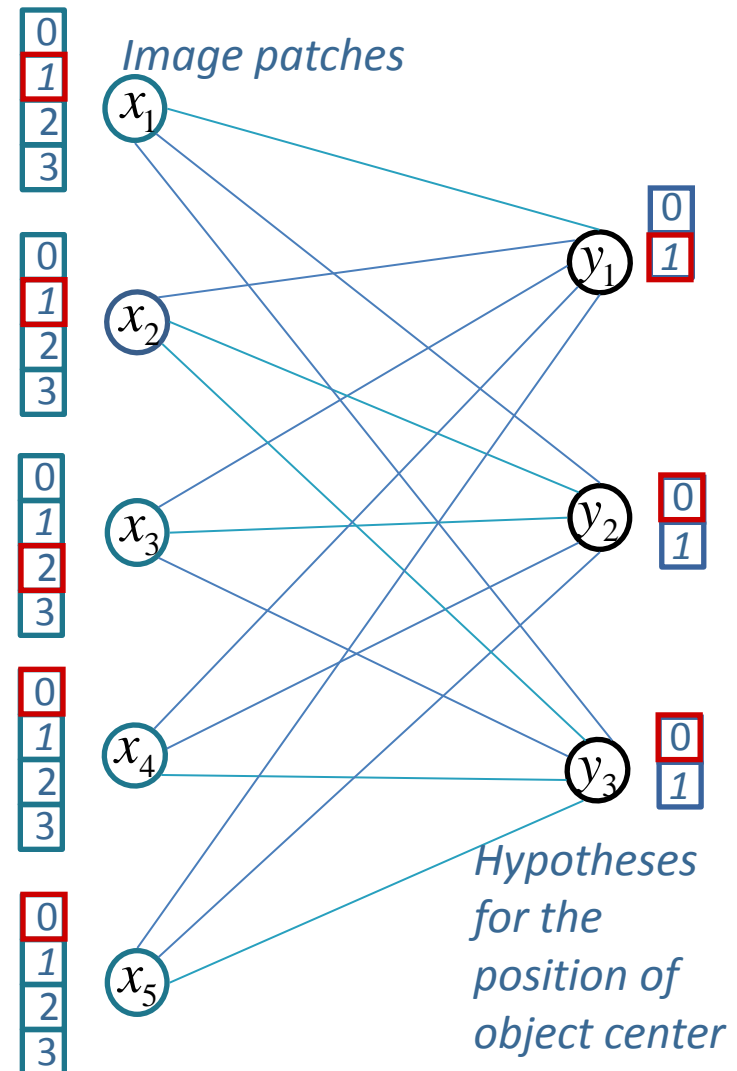
$y$  – labelling of hypotheses,  
 binary variables:  
 $y = 1$ , if the object is present,  
 $y = 0$ , otherwise

**Key idea : joint MAP-inference in  $x$  and  $y$**

Joint work with Victor Lempitsky and Pushmeet Kohli, CVPR10

# Occlusion constraint

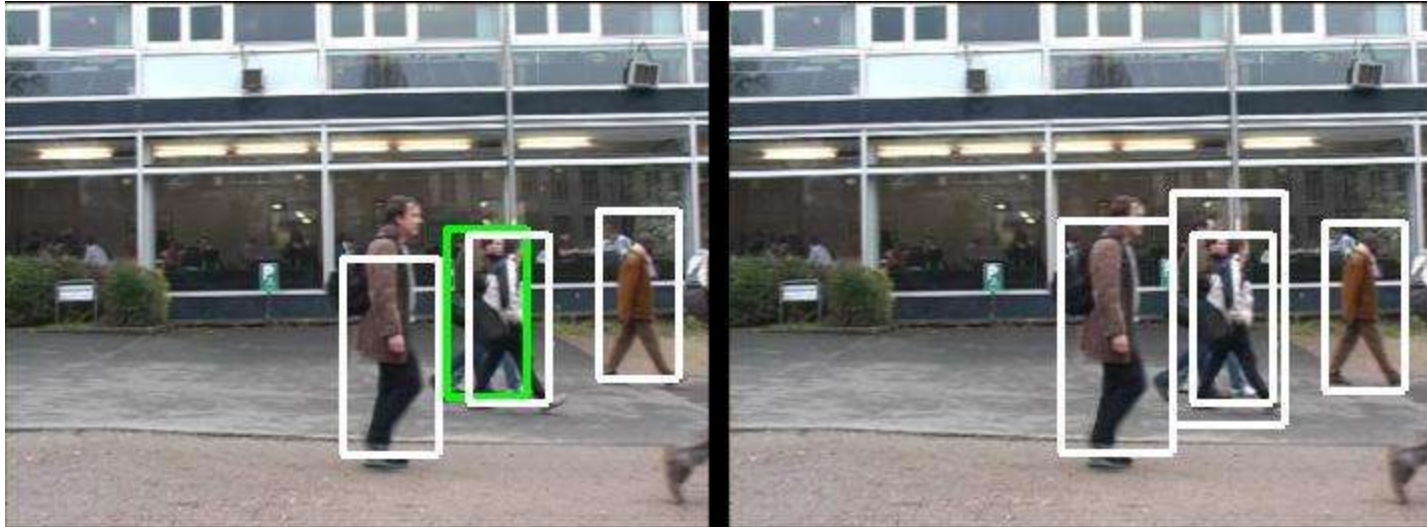
- Graphical model
  - If labeling of  $\mathbf{y}$  is fixed, the values of  $x_i$  are independent
  - So we can maximize  $\mathbf{x}$  out first and perform inference over  $\mathbf{y}$



Joint work with Victor Lempitsky and Pushmeet Kohli, CVPR10

# Occlusion constraint

- Comparison



Without occlusion constraint

Using occlusion constraint

White = correct detection

Green = missing object

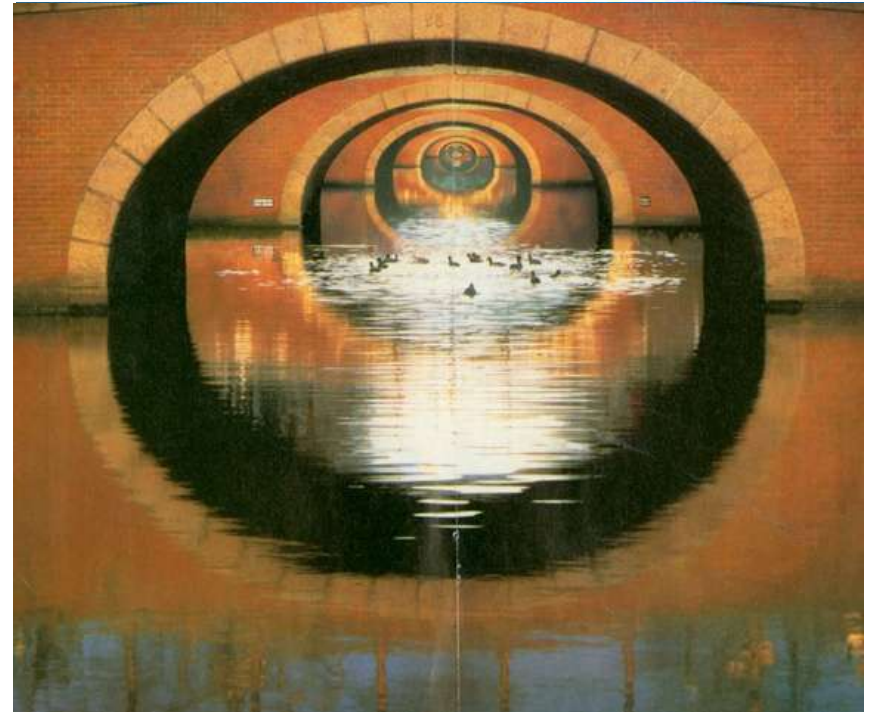
Red = false positive

Code available online!!!

Joint work with Victor Lempitsky and Pushmeet Kohli, CVPR10

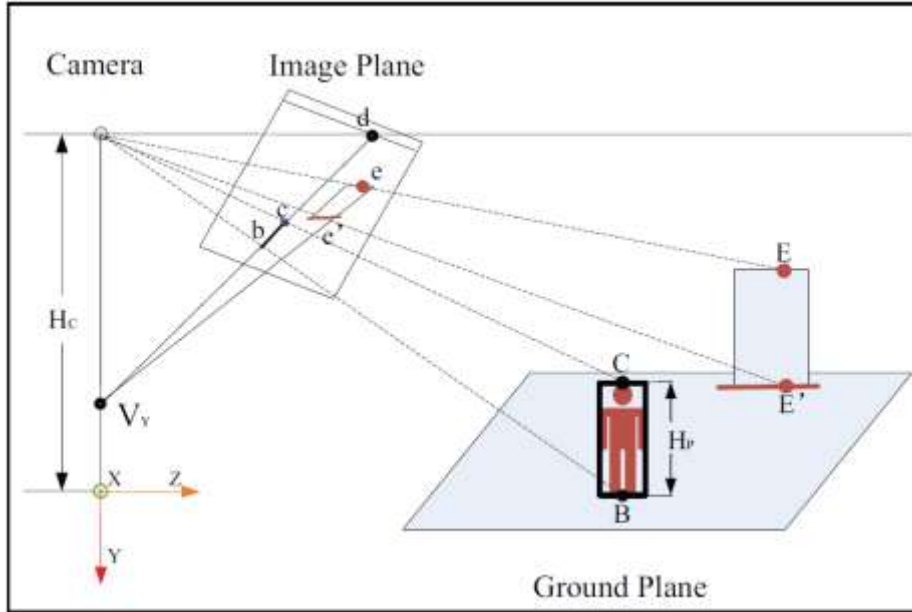


- Outline of the talk
  - The idea of graphical models
  - **Examples:**
    - Limiting the set of allowed deformations
    - Occlusion constraint
    - **Depth ordering constraint**
    - Modeling the rules of perspective geometry



# Expressing constraints with graphical models

- Depth ordering



- The size of an object depends on the distance from the viewpoint
- Viewpoint is set by the position of horizon and ground plane in the image

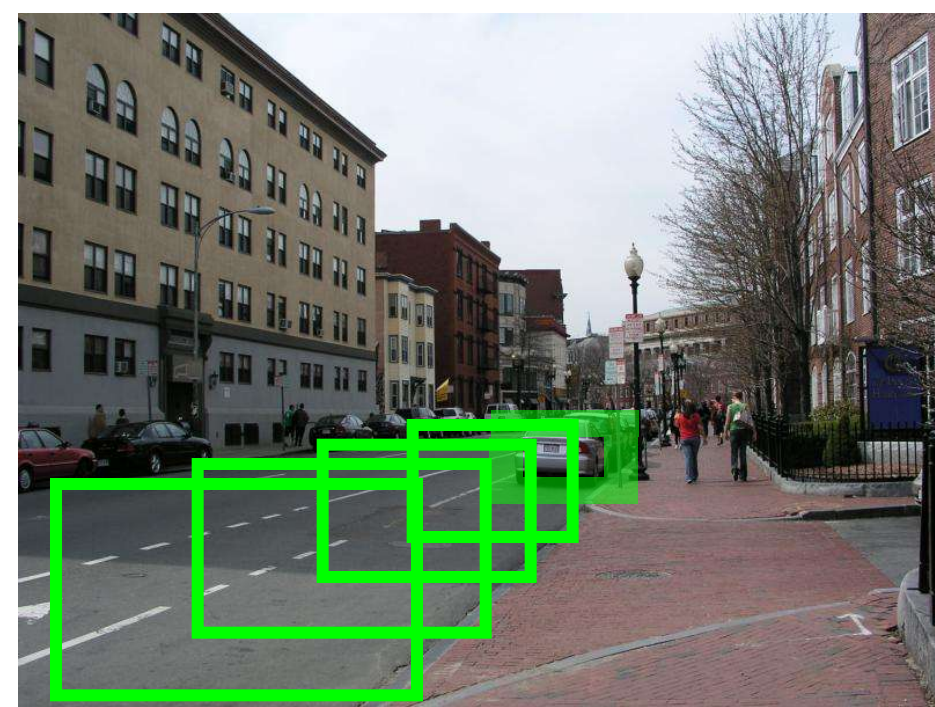


# Depth ordering constraint

- Viewpoint  $\rightarrow$  prior on the size of the objects

Object Position/Sizes

Viewpoint



Hoiem et al. , CVPR2006

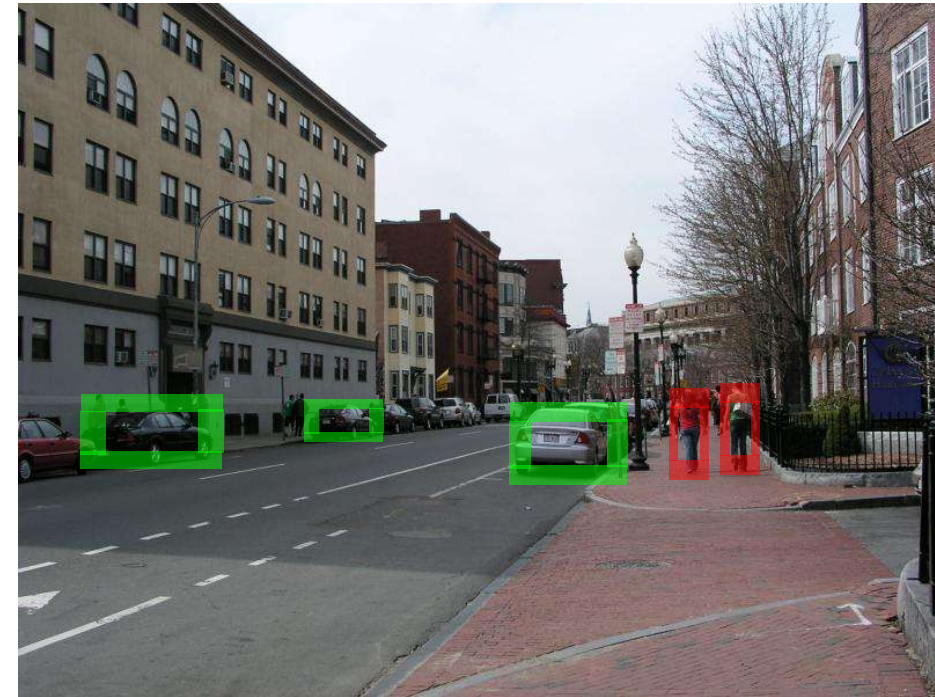
# Depth ordering constraint

- Detected objects  $\rightarrow$  viewpoint

Object Position/Sizes



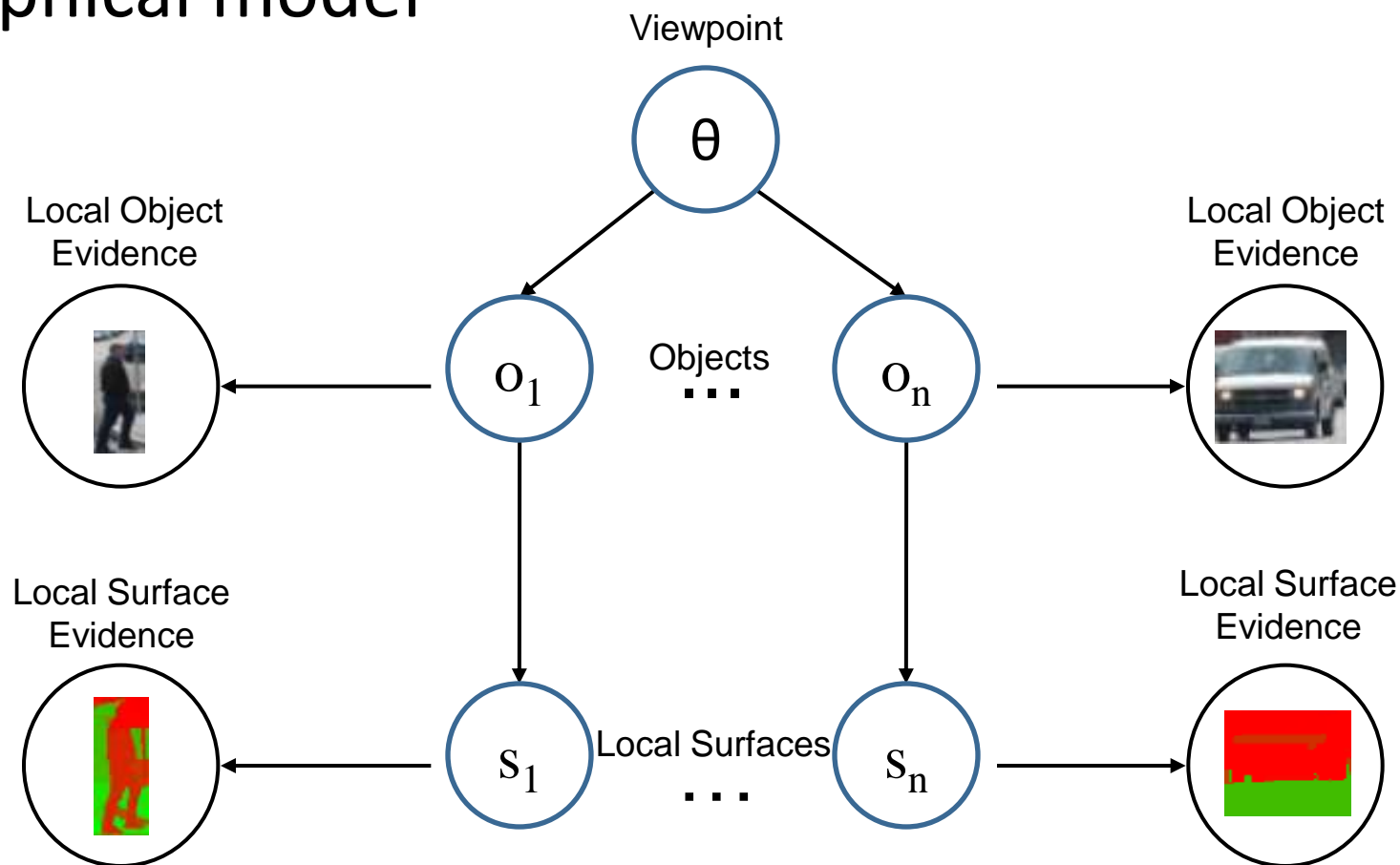
Viewpoint



Hoiem et al. , CVPR2006

# Depth ordering constraint

- Graphical model



Hoiem et al. , CVPR2006

# Depth ordering constraint

- Prior on the size and position of the objects



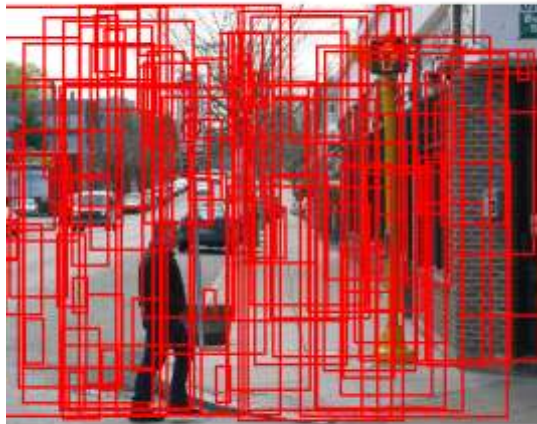
Image



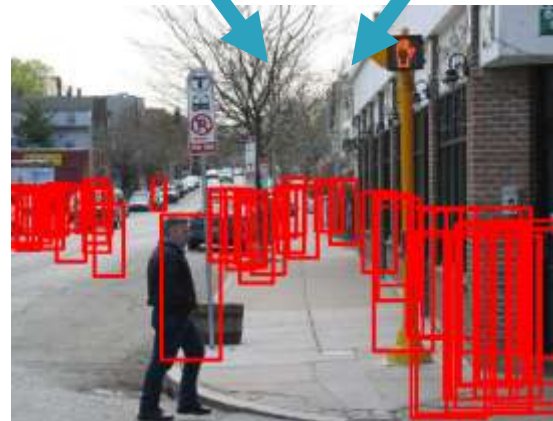
P(surfaces)



P(viewpoint)



P(object)

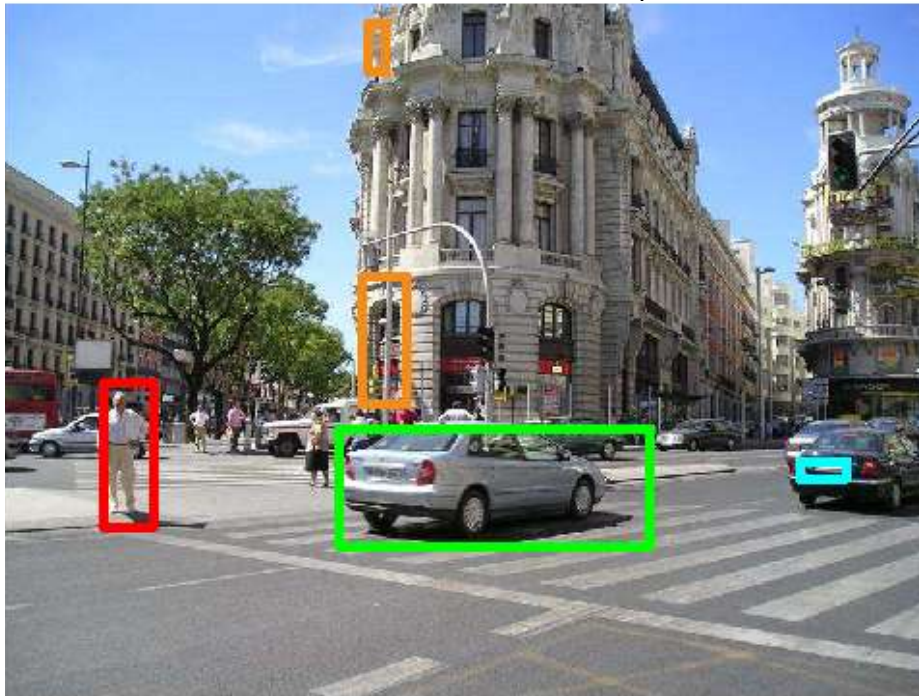


P(object | surfaces, viewpoint)

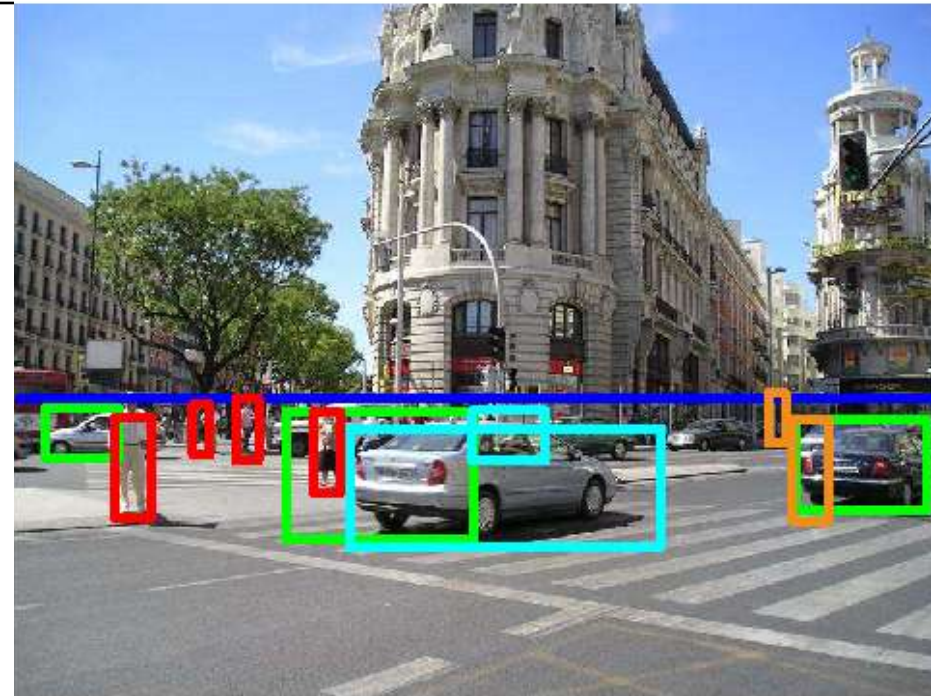
# Depth ordering constraint

- Comparison

Car: TP / FP Ped: TP / FP



Initial: 2 TP / 3 FP



Final: 7 TP / 4 FP

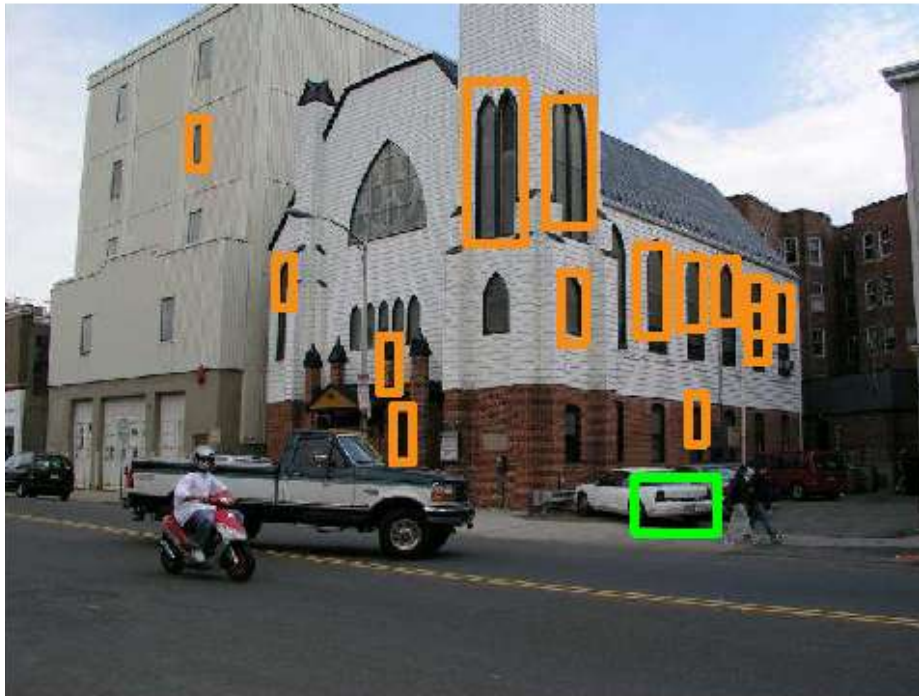
Hoiem et al. , CVPR2006

Local Detector from [Murphy-Torralla-Freeman 2003]

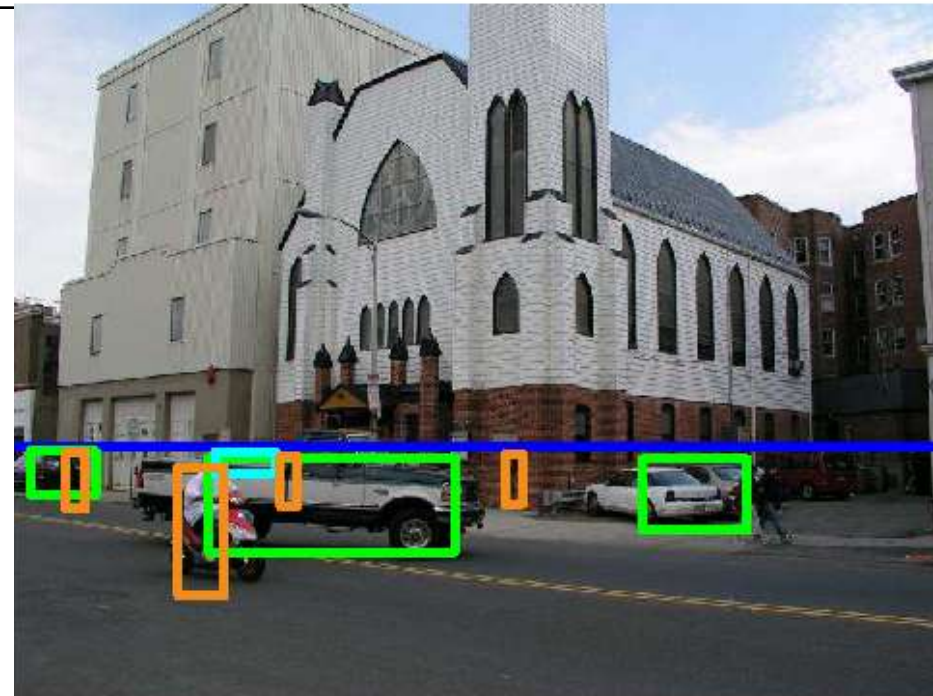
# Depth ordering constraint

- Comparison

Car: TP / FP Ped: TP / FP



Initial: 1 TP / 14 FP



Final: 3 TP / 5 FP

Hoiem et al. , CVPR2006

Local Detector from [Murphy-Torralla-Freeman 2003]



- Outline of the talk
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  - **Examples:**
    - Limiting the set of allowed deformations
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    - Depth ordering constraint
    - **Modeling the rules of perspective geometry**



- Rules of perspective geometry
  - Straight lines lying on parallel planes in 3D intersect in the image plane in **vanishing point**
  - Vanishing point corresponding to vertical lines is called **zenith**
  - All vanishing points which correspond to horizontal lines lie on the same straight line called **horizon**



# Modeling the rules of perspective geometry

- Geometric primitives and geometric parsing



Image of man-made environment



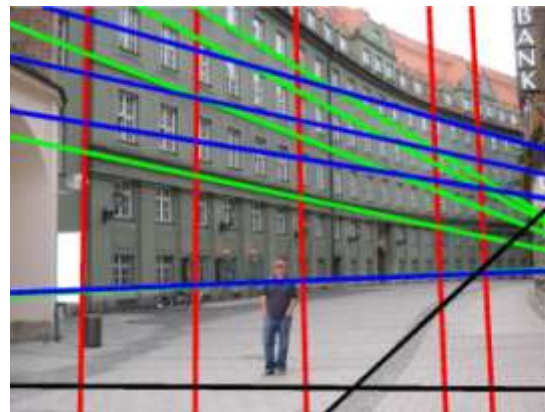
Edge pixels



Line segments



Lines



Vanishing points



Zenith and horizon

Joint work with Elena Tretyak, Victor Lempitsky and Pushmeet Kohli, ECCV10

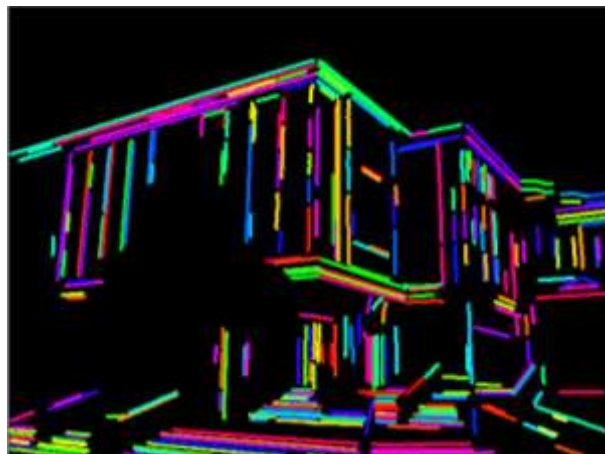
# Modeling the rules of perspective geometry

- Traditional approach: bottom-up pipeline

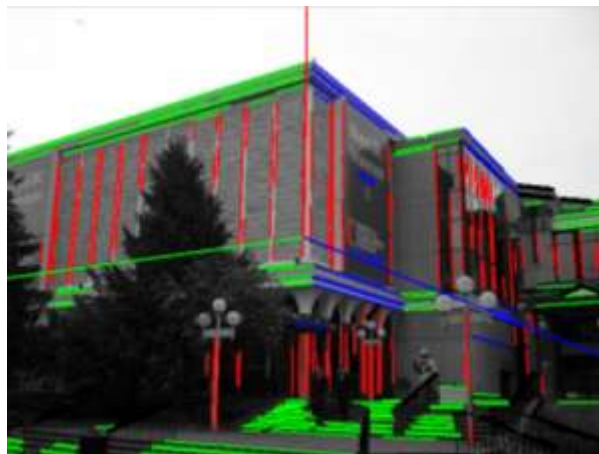
*Input image*



*Edge map*



1. *Grouping edge pixels into line segments*



2. *Grouping line segments and VPs estimation*



3. *Horizon and zenith estimation*

\*Tuytelaars 1998, Antone 2000, Almansa 2003, Aguilera 2005, Boulanger 2006, Tardif 2009



# Modeling the rules of perspective geometry

- Energy function

- All geometric primitives are detected in the simultaneously by energy minimization:

$$E_{total}(\mathbf{s}, \mathbf{l}, \mathbf{h}, z | \mathbf{p}) = \sum_{i=1..P} E_{edge}(p_i | \mathbf{s}) + \sum_{i=1..S} E_{segment}(s_i | \mathbf{l}) + \sum_{i=1..L} E_{line}(l_i | \mathbf{h}, z) + \sum_{1 \leq i < j \leq H} E_{horizon}(h_i, h_j | z) + E_{prior}(\mathbf{s}, \mathbf{l}, \mathbf{h}),$$

$\mathbf{p}$  – edge pixels,  $\mathbf{s}$  – line segments,  $\mathbf{l}$  – lines,  
 $z$  – zenith,  $\mathbf{h}$  – horizontal vanishing points

Joint work with Elena Tretyak, Victor Lempitsky and Pushmeet Kohli, ECCV10

# Modeling the rules of perspective geometry

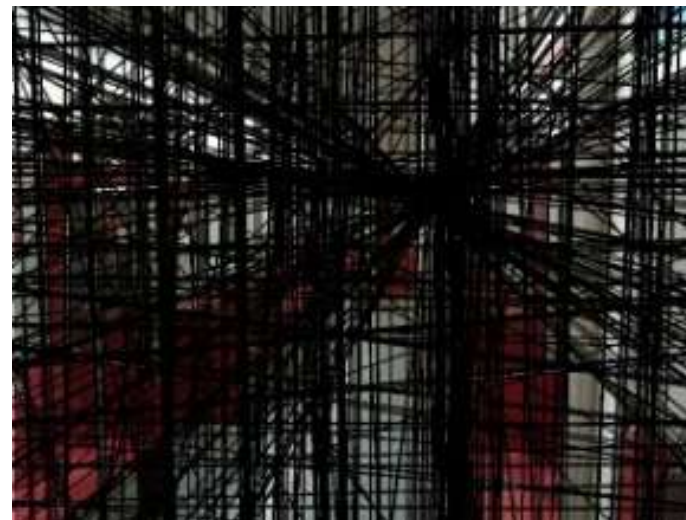


- Discretization of the model

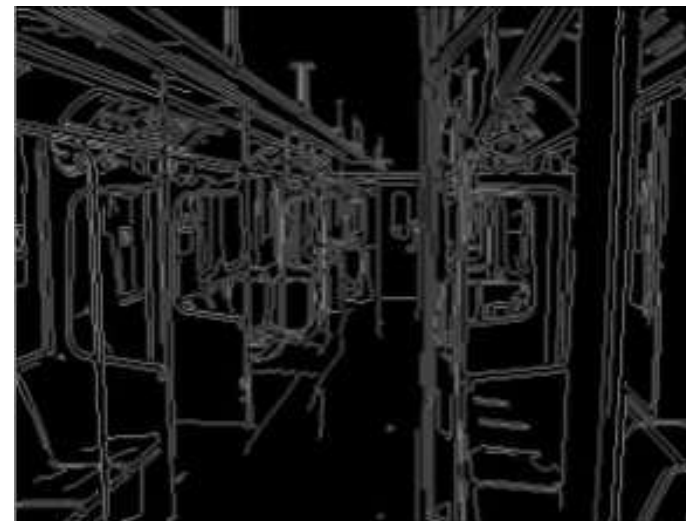
Candidate vanishing points



Candidate line segments



Candidate lines



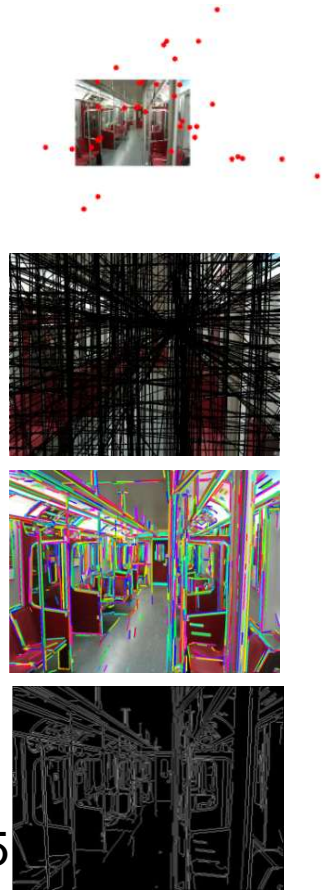
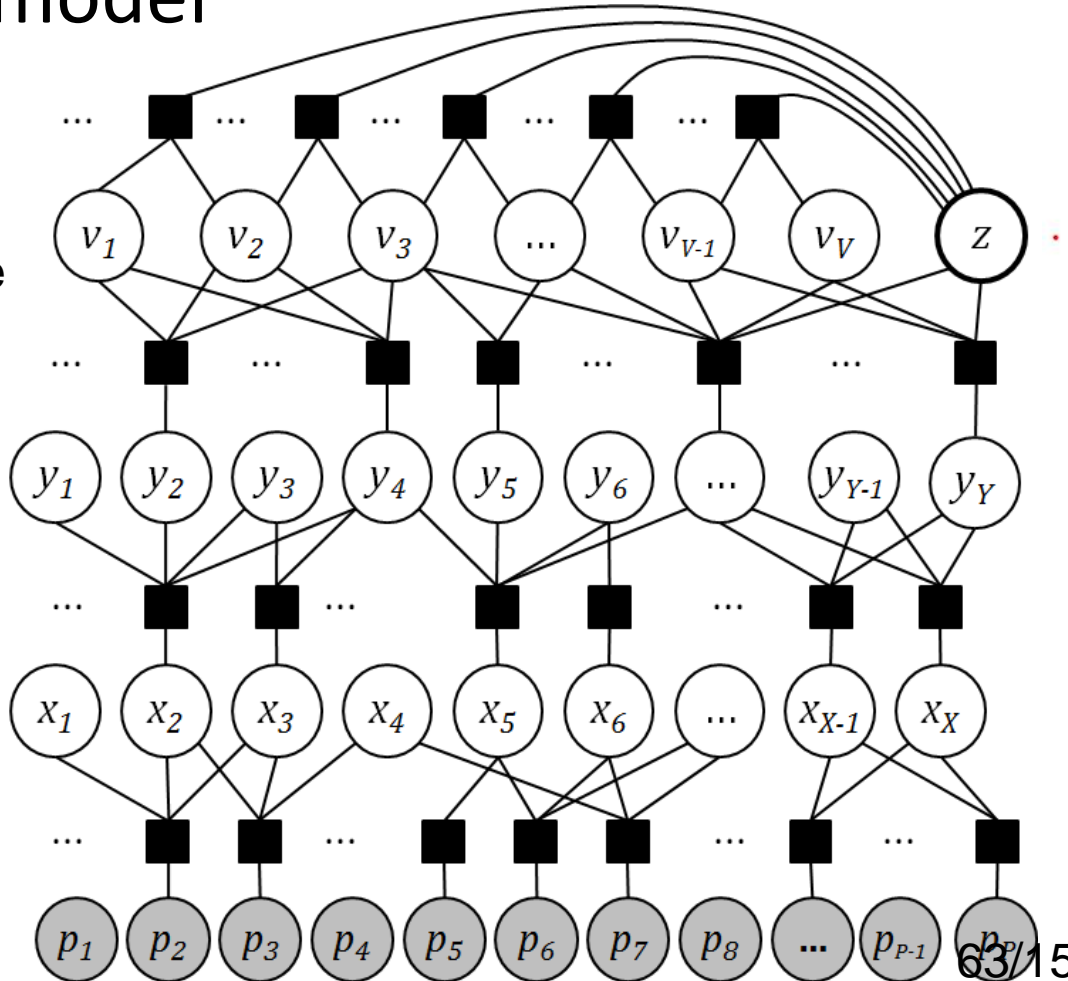
Candidate edge pixels

# Modeling the rules of perspective geometry

- Graphical model

■ – factors correspond to the potentials of the energy function

○ – nodes correspond to geometric primitives



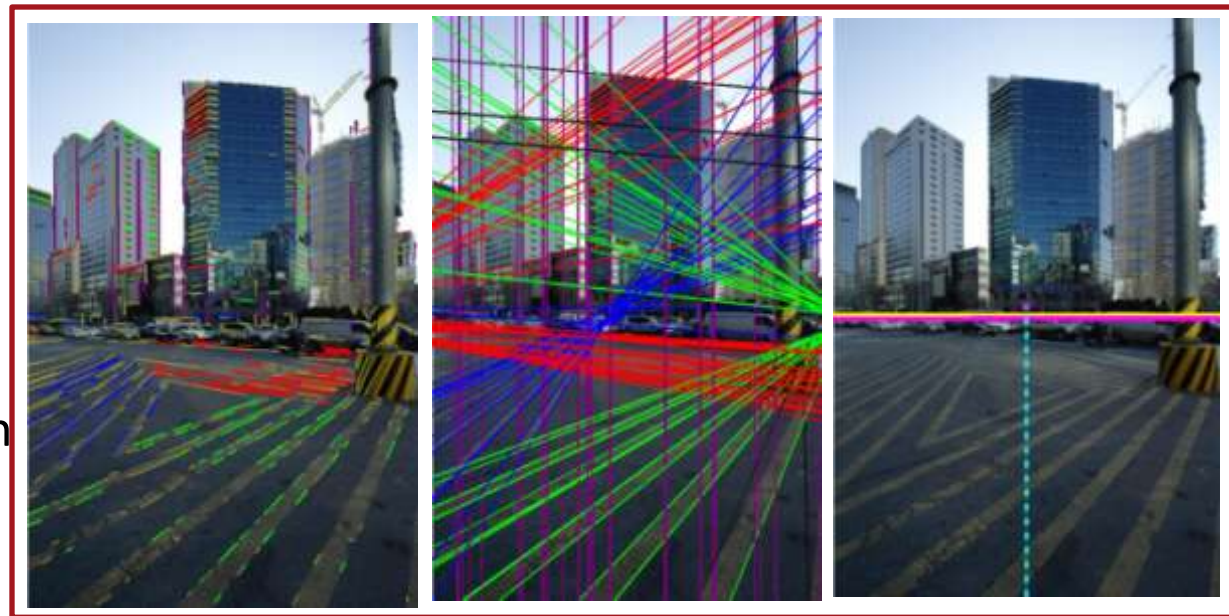
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# Modeling the rules of perspective geometry

- Results of geometric parsing



Energy  
minimization



Input image

Detected geometric primitives

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# Modeling the rules of perspective geometry

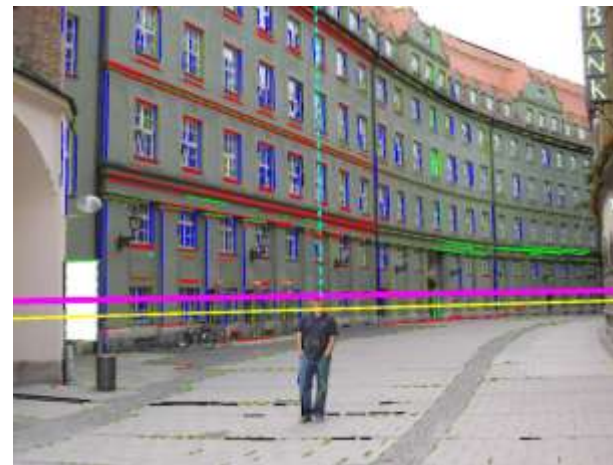


- Comparison



Result of geometric parsing  
with full energy

Code available online!!!



Omitting horizon constraint

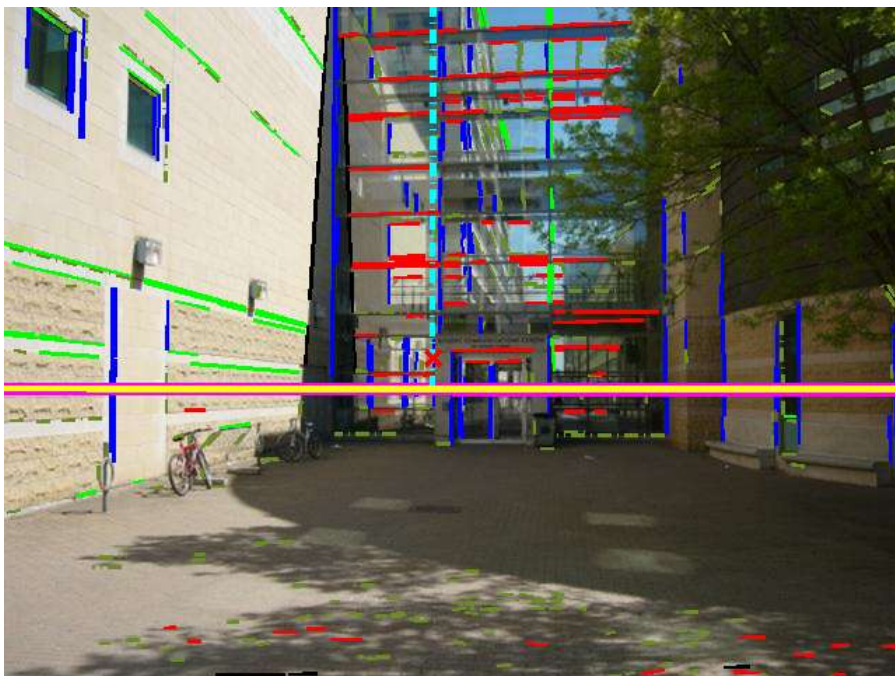


Bottom-up pipeline

# Modeling the rules of perspective geometry



- Comparison

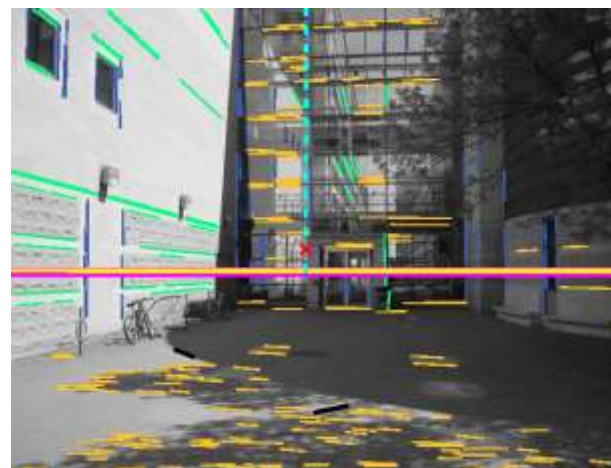


Result of geometric parsing  
with full energy

Code available online!!!



Omitting horizon constraint

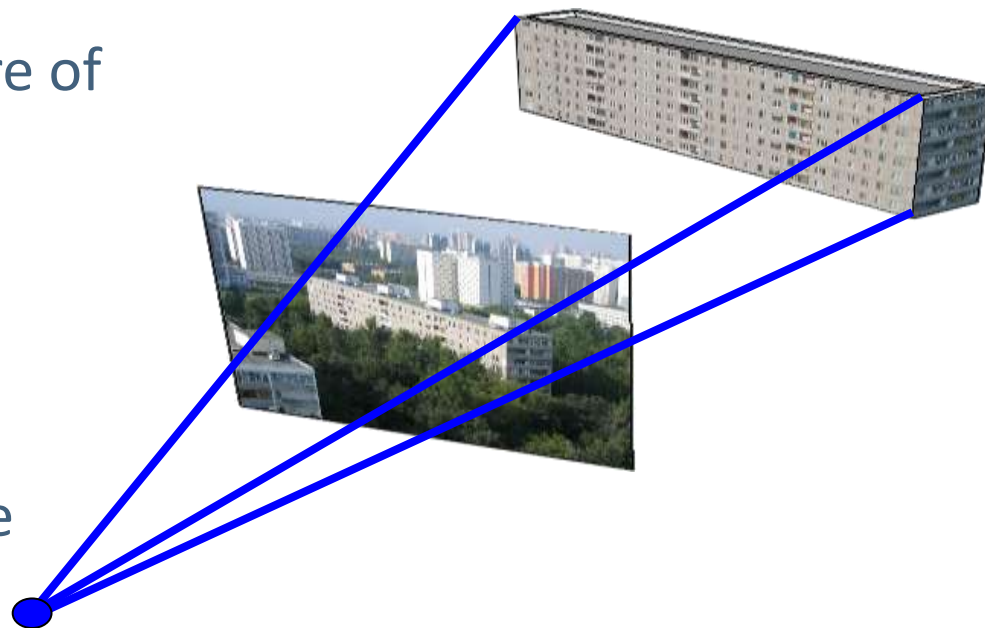


Bottom-up pipeline

# Modeling the rules of perspective geometry

- Application: single-view geometry

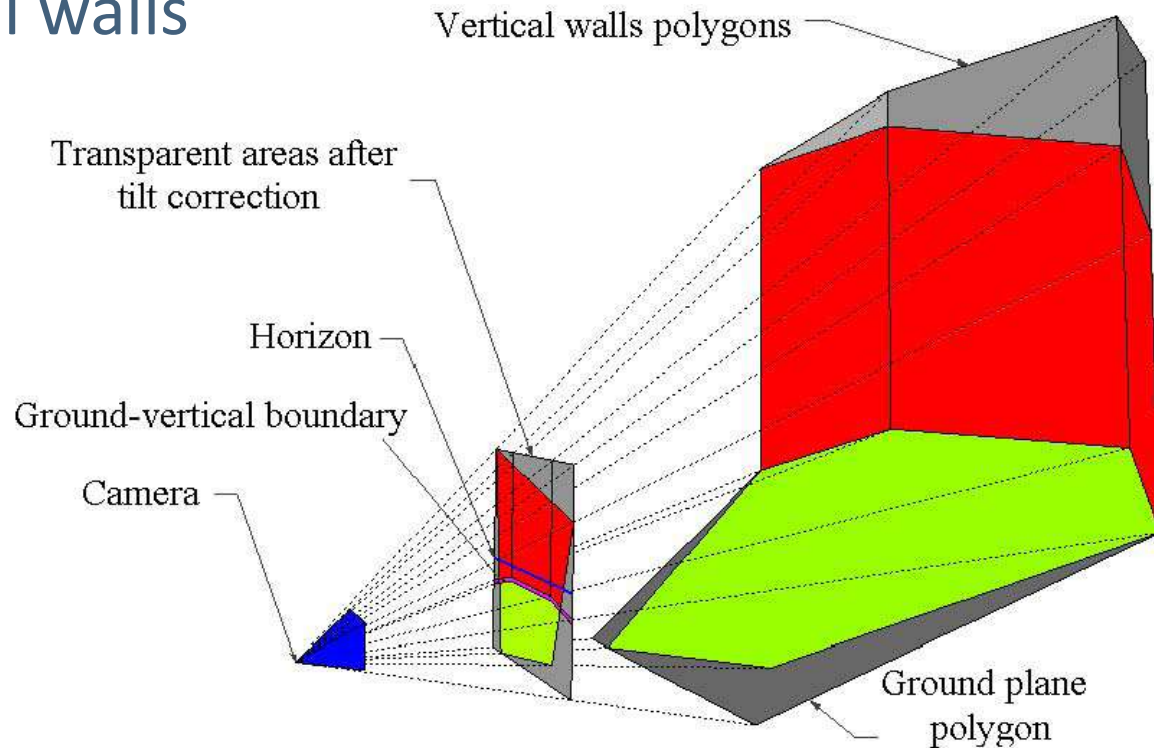
- 3-d reconstruction = recovering 3-d structure of the scene from its projection(s)
- Single-view 3-d reconstruction is an ill-posed problem, infinite number of possible solutions



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# Application: single-view geometry

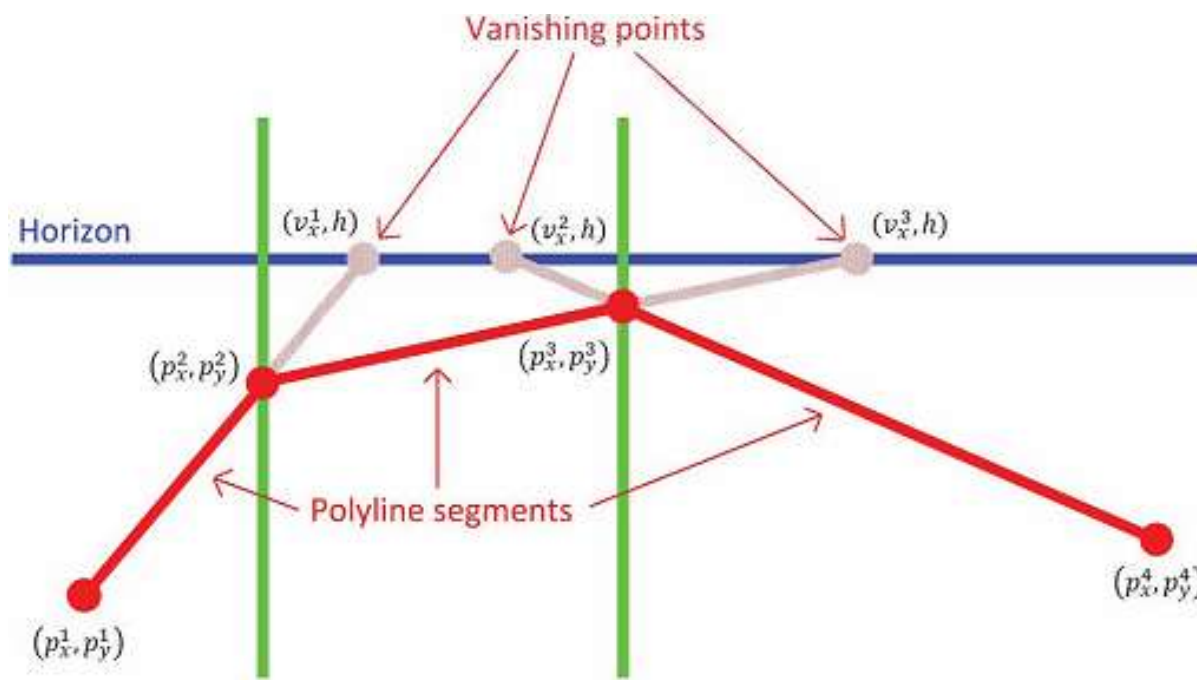
- The structure of 3d model
  - 3d model is composed of ground plane and a number of vertical walls



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# Application: single-view geometry

- The structure of 3d model



*Parameterization:*

- $(n-1)$  X-coordinates of polyline fractures  $p_x^i$ ,  $(i = 2, \dots, n)$
- $(n)$  X-coordinate of VP  $v_x^i$ ,  $(i = 1, \dots, n)$
- Horizon level  $h$
- Y-coordinate of polyline left end  $p_y^1$

# Application: single-view geometry

- Demo



single image



3d model

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# Thank you for attention!

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courses on computer vision at MSU