

Microsoft Research  
Faculty  
Summit  
**2016**



# Private Predictions with Homomorphic Encryption

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# Presentation Outline

Privacy in Prediction

SEAL

Examples



# Privacy in Prediction





Medical

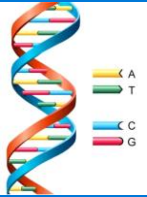
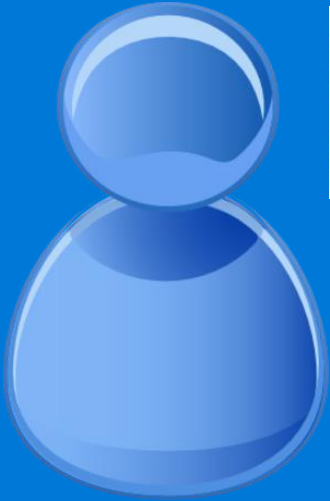


Genomic



Financial

Wait! What about Privacy?



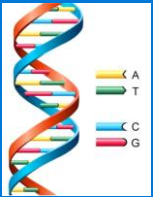
Who else is going to see your DNA sequence and the prediction?





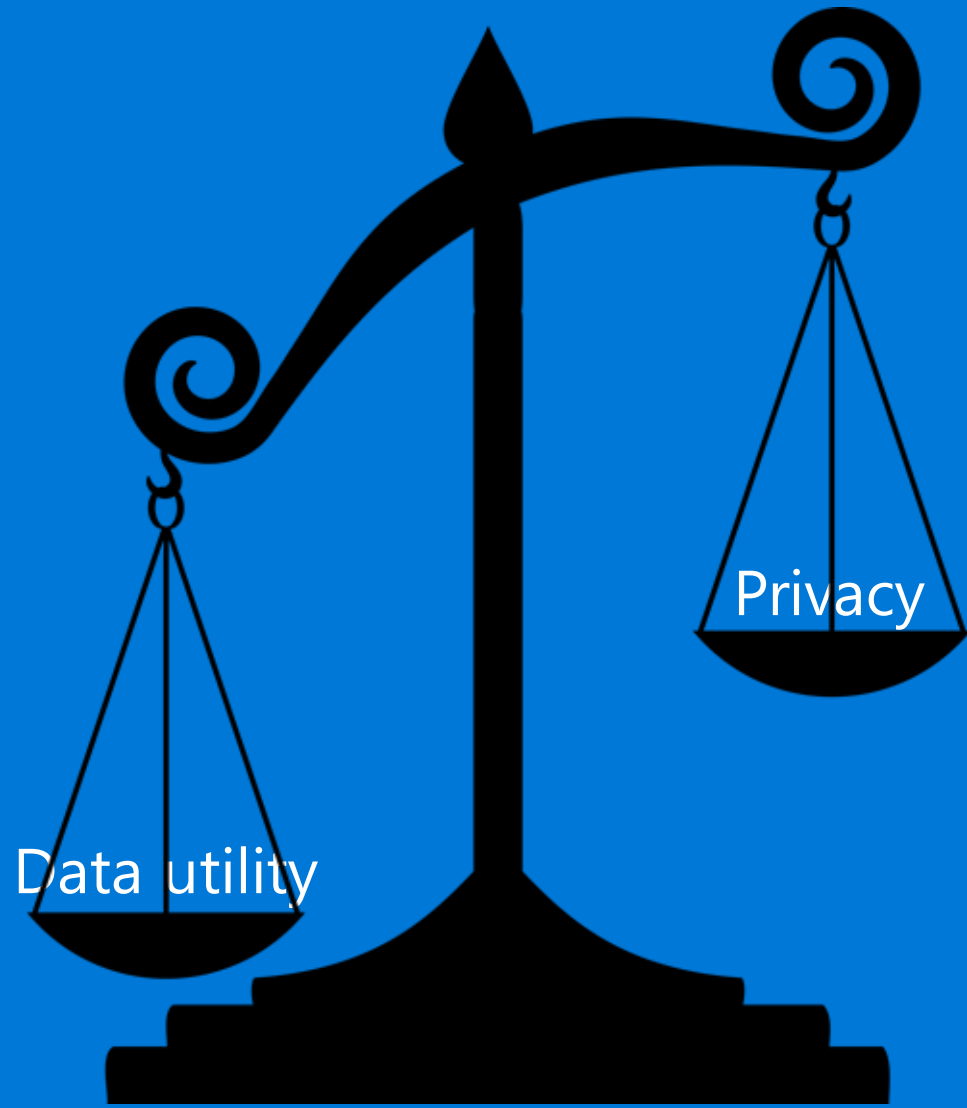
# Who else is going to see your DNA sequence and the prediction?

“Sorry, your DNA does not match this job description.”



“Here is an advertisement that according to your DNA you will not be able to resist.”

“We are not giving you this loan because it is not in your DNA to pay it back.”



Can encryption help?

Can encryption help?

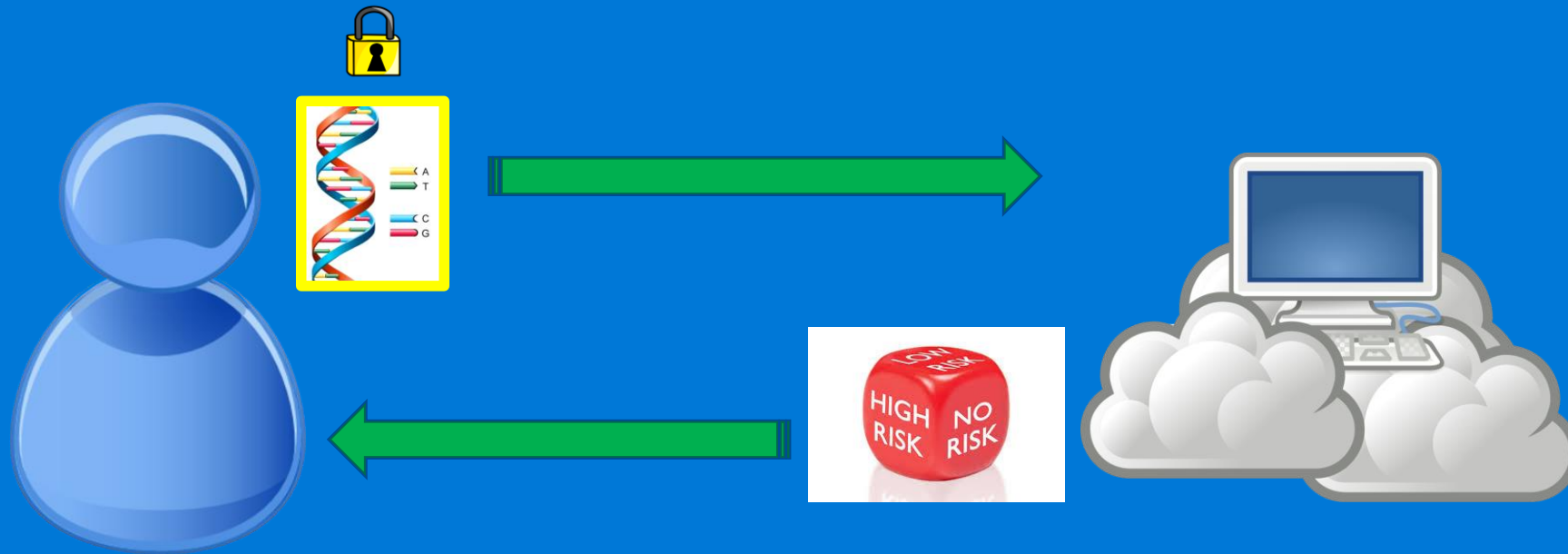
Possibly. But need *very* special type of encryption!

# Inference over encrypted data

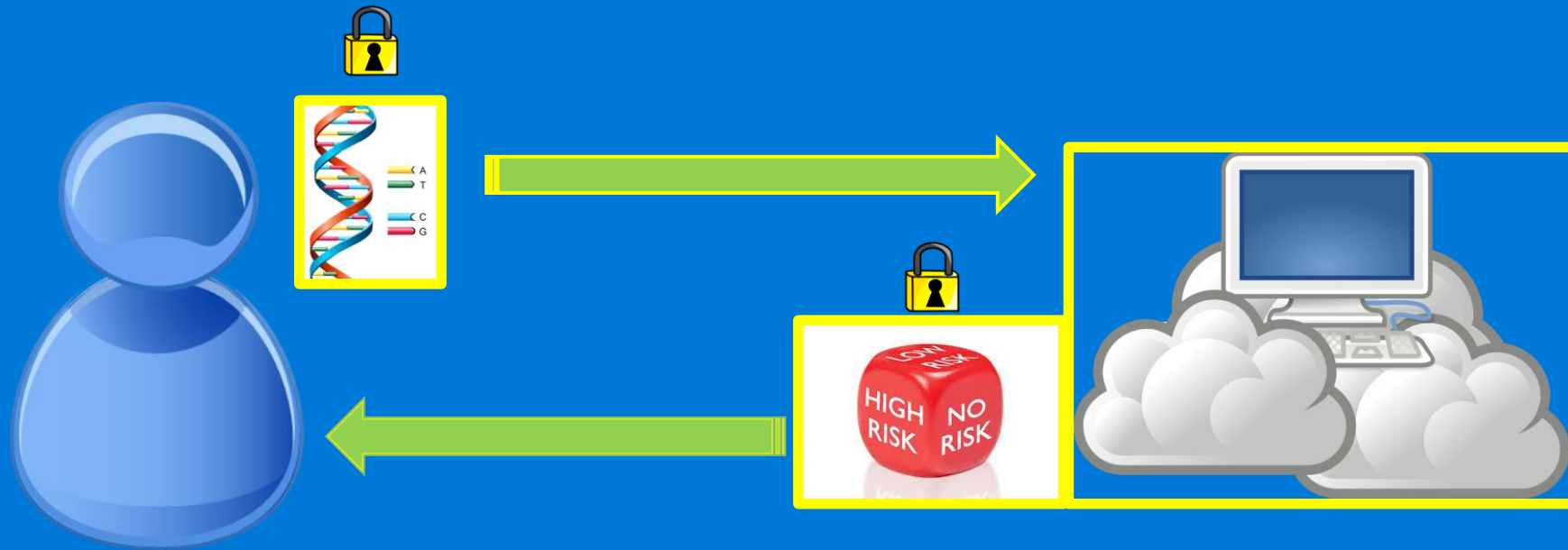




# Inference over encrypted data



# Inference over encrypted data



Can encryption help?

Possibly. But need *very* special type of encryption!

Can encryption help?

Possibly. But need *very* special type of encryption!

Yes. Homomorphic encryption.

# Fully Homomorphic Encryption Using Ideal Lattices

Craig Gentry

Stanford University and IBM Watson

cgentry@cs.stanford.edu

## ABSTRACT

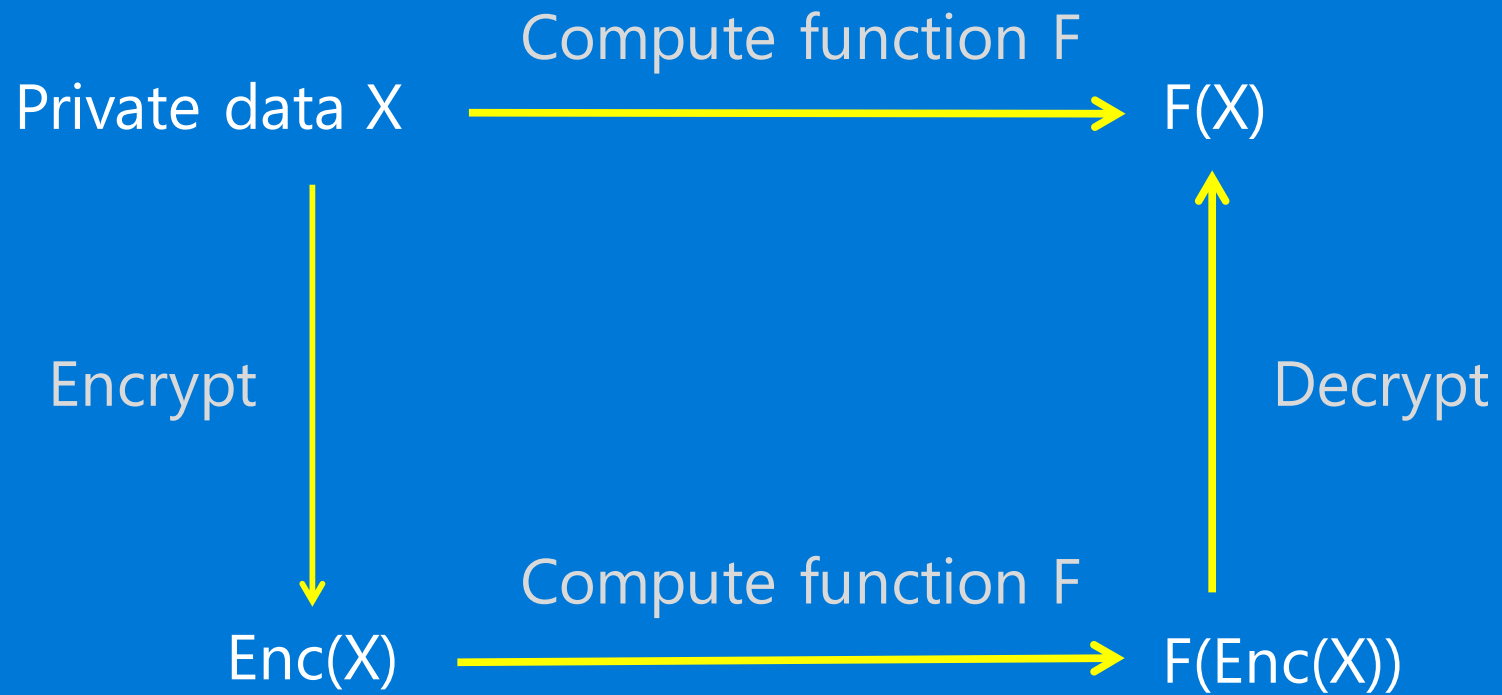
We propose a fully homomorphic encryption scheme – i.e., a scheme that allows one to evaluate circuits over encrypted data without being able to decrypt. Our solution comes in three steps. First, we provide a general result – that, to construct an encryption scheme that permits evaluation of *arbitrary circuits*, it suffices to construct an encryption scheme that can evaluate (slightly augmented versions of) its *own decryption circuit*; we call a scheme that can evaluate its (augmented) decryption circuit *bootstrappable*.

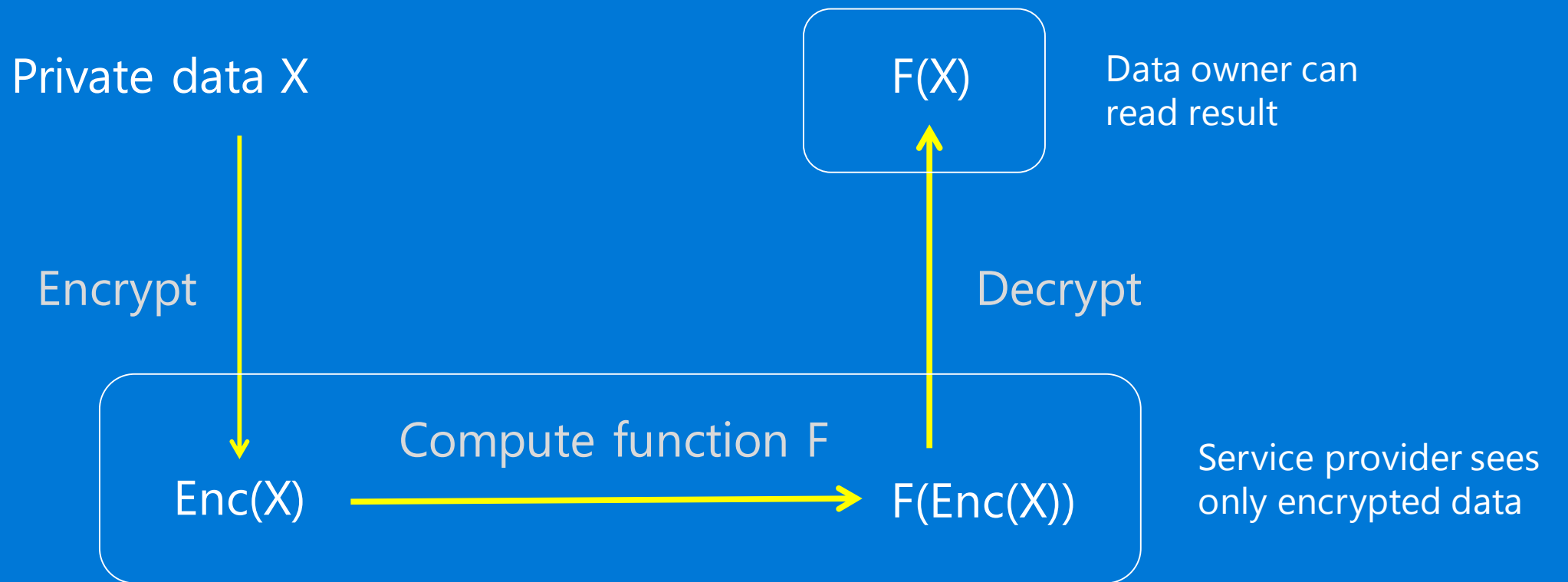
Next, we describe a public key encryption scheme using *ideal lattices* that is *almost* bootstrappable. Lattice-based cryptosystems typically have decryption algorithms with low

duced by Rivest, Adleman and Dertouzos [54] shortly after the invention of RSA by Rivest, Adleman and Shamir [55]. Basic RSA is a multiplicatively homomorphic encryption scheme – i.e., given RSA public key  $pk = (N, e)$  and ciphertexts  $\{\psi_i \leftarrow \pi_i^e \bmod N\}$ , one can efficiently compute  $\prod_i \psi_i = (\prod_i \pi_i)^e \bmod N$ , a ciphertext that encrypts the product of the original plaintexts. Rivest et al. [54] asked a natural question: What can one do with an encryption scheme that is *fully* homomorphic: a scheme  $\mathcal{E}$  with an efficient algorithm  $\text{Evaluate}_{\mathcal{E}}$  that, for any valid public key  $pk$ , *any* circuit  $C$  (not just a circuit consisting of multiplication gates), and any ciphertexts  $\psi_i \leftarrow \text{Encrypt}_{\mathcal{E}}(pk, \pi_i)$ , output

$$\psi \leftarrow \text{Evaluate}_{\mathcal{E}}(pk, C, \psi_1, \dots, \psi_t),$$







$F(X)$  must be a polynomial in the data  $X$

Private data  $X$

Encrypt

$\text{Enc}(X)$

Compute function  $F$

$F(\text{Enc}(X))$

Decrypt

$F(X)$

Data owner can read result

Service provider sees only encrypted data

# SEAL

# Simple Encrypted Arithmetic Library – SEAL

*Easy-to-use homomorphic encryption library*





Homomorphic encryption library by MSR Cryptography Research group  
Focus on ease-of-use, good API design, good engineering  
Written in C++11  
Contains .NET wrappers for entire public API  
Source code publicly available  
Under active development

<http://sealcrypto.codeplex.com>



Choose encryption parameters

Create public and secret keys

Encrypt some integers (encode + encrypt)

Do homomorphic evaluation

Decrypt the results (decrypt + decode)

```
void simple_example()
{
    EncryptionParameters parms;
    parms.poly_modulus() = "1x^2048 + 1";
    parms.coeff_modulus() = ChooserEvaluator::default_parameter_options().at(2048);
    parms.plain_modulus() = 1 << 10;

    KeyGenerator keygen(parms);
    keygen.generate();
    auto public_key = keygen.public_key();
    auto secret_key = keygen.secret_key();

    BinaryEncoder encoder(parms.plain_modulus());
    Encryptor encryptor(parms, public_key);
    auto plain1 = encoder.encode(5);
    auto plain2 = encoder.encode(7);
    auto enc1 = encryptor.encrypt(plain1);
    auto enc2 = encryptor.encrypt(plain2);

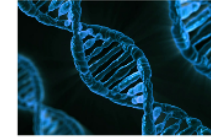
    Evaluator evaluator(parms);
    auto enc_product = evaluator.multiply(enc1, enc2);
    auto enc_sum = evaluator.add(enc1, enc2);

    Decryptor decryptor(parms, secret_key);
    auto plain_product = decryptor.decrypt(enc_product);
    auto plain_sum = decryptor.decrypt(enc_sum);
    uint64_t product = encoder.decode_uint64(plain_product);
    uint64_t sum = encoder.decode_uint64(plain_sum);

    cout << product << " " << sum << endl;
}
```

# Examples

# Genomic Predictor



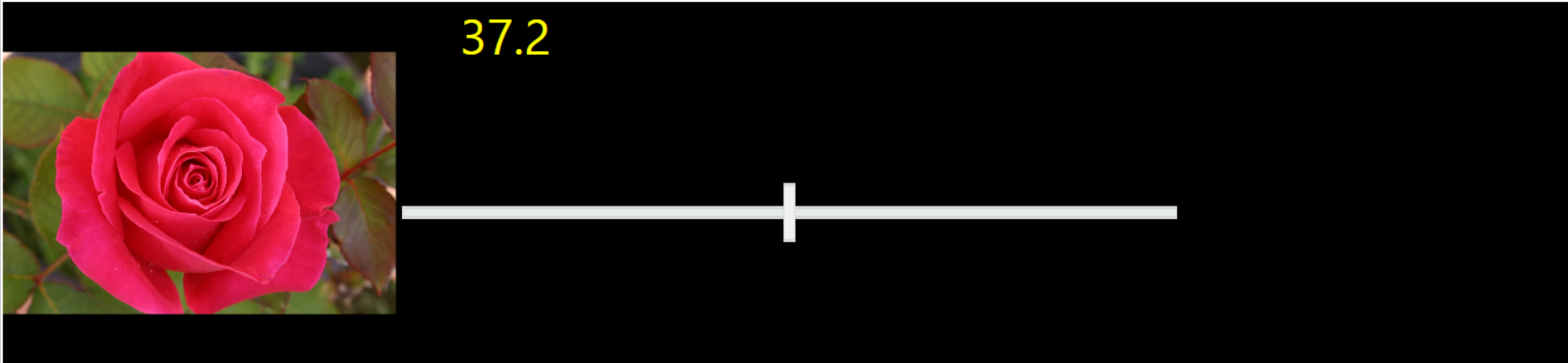
Clear

Next

Sending Request

Server Processing  
---.--- seconds

Decrypting Results  
---.--- seconds



acagagtgctgattgggtgcatttacaatcctctagctagacataaaaagttctccaagtccccactagattagctagagacacagagcactgatcag  
tgatttacaacacagagtgctgattgggtgcatttacaatcctctagctagacataaaaagttctccaagtccccactagattagctagagaca  
cagagcactgatcagtgatttacaacacagagtgctgattgggtgcatttacaatcctctagctagacataaaaagttctccaagtccccacta  
gattagctagagacacagagcactgatcagtgatttacaacacagagtgctgattgggtgcatttacaatcctctagctagacataaaaagtt  
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ctagacataaaaagttctccaagtccccactagattagctagagacacagagcactgatcagtgatttacaacacagagtgctgattgggtgc  
atttacaatcctctagctagacataaaaagttctccaagtccccactagattagctagagacacagagcactgatcagtgatttacaacacag  
agtgctgattgggtgcatttacaatcctctagctagacataaaaagttctccaagtccccactagattagctagagacacagagcactgatcagtgca  
cagagtgctgattgggtgcatttacaatcctctagctagacataaaaagttctccaagtccccactagattagctagagacacagagcactgatcagtgca


## 200K SNPs

Demo

SEAL demonstrations

Genomics Pneumonia CryptoNets Interactive Manage

# Pneumonia Risk Calculator



**Clear**

**Next**

**Sending Request**

---.--- seconds

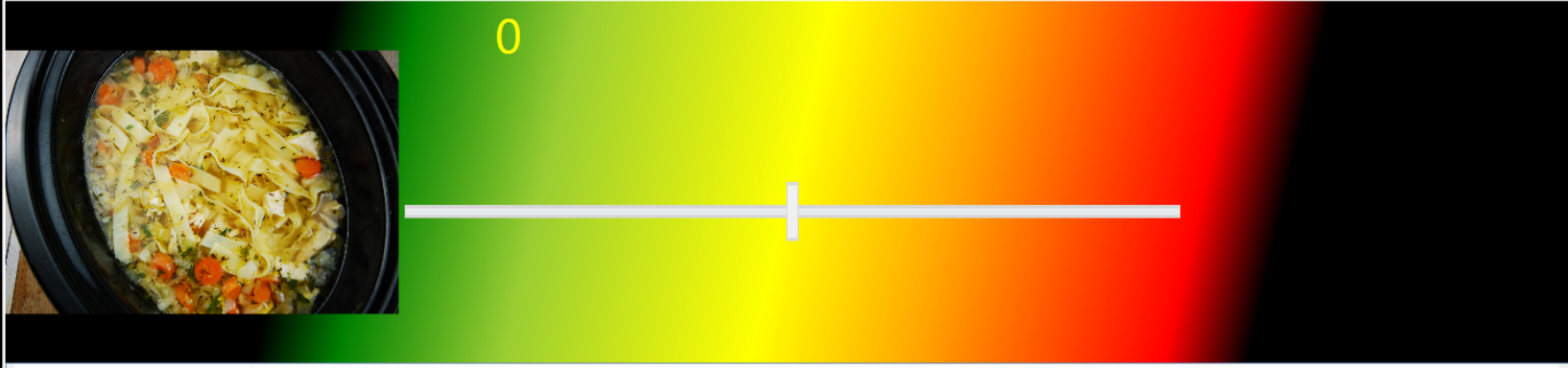
**Server Processing**

---.--- seconds

**Decrypting Results**

---.--- seconds

0



Attribute	
age	
gender	
admitted_through_ER	
history_of_chest_pain	
chronic_lung_disease	
asthma	

ccagagtcctgaattggtgcatttacaatccctctagctagacataaaagtctcccaagtcctccactagatt

Demo: Pneumonia Risk Prediction





# CryptoNets

# Thank you!

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