Deep Reinforcement Learning via Policy Optimization

John Schulman

OpenAl

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Introduction

Deep Reinforcement Learning: What to Learn?

Policies (select next action)

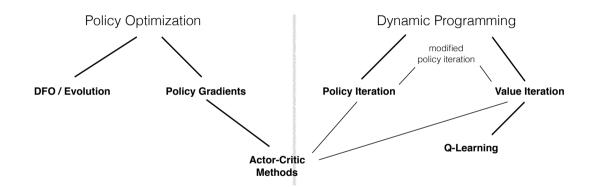
Deep Reinforcement Learning: What to Learn?

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- ▶ Value functions (measure goodness of states or state-action pairs)

Deep Reinforcement Learning: What to Learn?

- ▶ Policies (select next action)
- Value functions (measure goodness of states or state-action pairs)
- Models (predict next states and rewards)

Model Free RL: (Rough) Taxonomy



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- ► Empirically . . .
 - ► Policy optimization more versatile, dynamic programming methods more sample-efficient when they work
 - Policy optimization methods more compatible with rich architectures (including recurrence) which add tasks other than control (auxiliary objectives), dynamic programming methods more compatible with exploration and off-policy learning

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 - Continuous action space: network outputs mean and diagonal covariance of Gaussian

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 - ► Taxi robot reaches its destination (termination = good)
 - Waiter robot finishes a shift (fixed time)
 - Walking robot falls over (termination = bad)
- ► Goal: maximize expected return per episode

$$\mathop{\rm maximize}_{\pi} \mathbb{E}\left[R \mid \pi\right]$$

Derivative Free Optimization / Evolution

```
Initialize \mu \in \mathbb{R}^d, \sigma \in \mathbb{R}^d for iteration =1,2,\ldots do Collect n samples of \theta_i \sim \mathit{N}(\mu, \operatorname{diag}(\sigma)) Perform one episode with each \theta_i, obtaining reward R_i Select the top p\% of \theta samples (e.g. p=20), the elite set Fit a Gaussian distribution, to the elite set, updating \mu, \sigma. end for Return the final \mu.
```

Sometimes works embarrassingly well

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| Method | Mean Score | Reference |
|----------------------------------|------------|---|
| Nonreinforcement learning | | |
| Hand-coded | 631,167 | Dellacherie (Fahey, 2003) |
| Genetic algorithm | 586,103 | (Böhm et al., 2004) |
| Reinforcement learning | | |
| Relational reinforcement | ≈50 | Ramon and Driessens (2004) |
| learning+kernel-based regression | | |
| Policy iteration | 3183 | Bertsekas and Tsitsiklis (1996 |
| Least squares policy iteration | <3000 | Lagoudakis, Parr, and Littman (2002) |
| Linear programming + Bootstrap | 4274 | Farias and van Roy (2006) |
| Natural policy gradient | ≈6800 | Kakade (2001) |
| CE+RL | 21,252 | |
| CE+RL, constant noise | 72,705 | |
| CE+RL, decreasing noise | 348,895 | |

I. Szita and A. Lörincz. "Learning Tetris using the noisy

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Approximate Dynamic Programming Finally Performs Well in the Game of Tetris

Victor Gabillon INRIA Lille - Nord Europe, Team SequeL, FRANCE victor.gabillon@inria.fr

Mohammad Ghavamzadeh* INRIA Lille - Team SequeL & Adobe Research mohammad.ghavamzadeh@inria.fr Bruno Scherrer INRIA Nancy - Grand Est, Team Maia, FRANCE bruno.scherrer@inria.fr

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"Score function" gradient estimator:

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Cross entropy method:

Connection to Finite Differences

▶ Suppose P_{μ} is Gaussian distribution with mean μ , covariance $\sigma^2 I$

$$\log P_{\mu}(\theta) = -\|\mu - \theta\|^2 / 2\sigma^2 + const$$

$$\nabla_{\mu} \log P_{\mu}(\theta) = (\theta - \mu) / \sigma^2$$

$$R_i \nabla_{\mu} \log P_{\mu}(\theta_i) = R_i (\theta_i - \mu) / \sigma^2$$

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Suppose we do *antithetic sampling*, where we use pairs of samples $\theta_+ = \mu + \sigma z$, $\theta_- = \mu - \sigma z$

$$\begin{split} &\frac{1}{2}\bigg(R(\mu+\sigma z,\zeta)\nabla_{\mu}\log P_{\mu}(\theta_{+})+R(\mu-\sigma z,\zeta')\nabla_{\mu}\log P_{\mu}(\theta_{-})\bigg)\\ &=\frac{1}{\sigma}\big(R(\mu+\sigma z,\zeta)-R(\mu-\sigma z,\zeta')\big)z \end{split}$$

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• Using same noise ζ for both evaluations reduces variance



Deriving the Score Function Estimator

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Derive by writing expectation as an integral

$$\nabla_{\mu} \int d\mu d\zeta \ P_{\mu}(\theta) R(\theta, \zeta)$$

$$= \int d\mu d\zeta \ \nabla_{\mu} P_{\mu}(\theta) R(\theta, \zeta)$$

$$= \int d\mu d\zeta \ P_{\mu}(\theta) \nabla_{\mu} \log P_{\mu}(\theta) R(\theta, \zeta)$$

$$= \mathbb{E}_{\theta, \zeta} \left[\nabla_{\mu} \log P_{\mu}(\theta) R(\theta, \zeta) \right]$$

Evolution strategies (Rechenberg and Eigen, 1973)

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- ▶ Reward weighted regression (Peters and Schaal, 2007), PoWER (Kober and Peters, 2007)

Success Stories

► CMA is very effective for optimizing low-dimensional locomotion controllers

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 - ▶ UT Austin Villa: RoboCup 2012 3D Simulation League Champion



Optimizing Walking Controllers for Uncertain Inputs and Environments

Jack M. Wang David J. Fleet Aaron Hertzmann University of Toronto











Success Stories

- CMA is very effective for optimizing low-dimensional locomotion controllers
 - ▶ UT Austin Villa: RoboCup 2012 3D Simulation League Champion



► Evolution Strategies was shown to perform well on Atari, competetive with policy gradient methods (Salimans et al., 2017)

Policy Gradient Methods

Problem:

maximize
$$E[R \mid \pi_{\theta}]$$

▶ Here, we'll use a fixed policy parameter θ (instead of sampling $\theta \sim P_{\mu}$) and estimate gradient with respect to θ

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- ▶ Here, we'll use a fixed policy parameter θ (instead of sampling $\theta \sim P_{\mu}$) and estimate gradient with respect to θ
- ▶ Noise is in action space rather than parameter space

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Intuitions: collect a bunch of trajectories, and ...

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- 1. Make the good trajectories more probable
- 2. Make the good actions more probable
- 3. Push the actions towards better actions

Score Function Gradient Estimator for Policies

► Now random variable is a whole trajectory

$$\tau = (s_0, a_0, r_0, s_1, a_1, r_1, \dots, s_{T-1}, a_{T-1}, r_{T-1}, s_T)$$

$$\nabla_{\theta} E_{\tau}[R(\tau)] = E_{\tau}[\nabla_{\theta} \log P(\tau \mid \theta)R(\tau)]$$

Score Function Gradient Estimator for Policies

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▶ Just need to write out $P(\tau \mid \theta)$:

$$P(\tau \mid \theta) = \mu(s_0) \prod_{t=0}^{T-1} [\pi(a_t \mid s_t, \theta) P(s_{t+1}, r_t \mid s_t, a_t)]$$

$$\log P(\tau \mid \theta) = \log \mu(s_0) + \sum_{t=0}^{T-1} [\log \pi(a_t \mid s_t, \theta) + \log P(s_{t+1}, r_t \mid s_t, a_t)]$$

$$\nabla_{\theta} \log P(\tau \mid \theta) = \nabla_{\theta} \sum_{t=0}^{T-1} \log \pi(a_t \mid s_t, \theta)$$

$$\nabla_{\theta} \mathbb{E}_{\tau} [R] = \mathbb{E}_{\tau} \left[R \nabla_{\theta} \sum_{t=0}^{T-1} \log \pi(a_t \mid s_t, \theta) \right]$$

Policy Gradient: Use Temporal Structure

Previous slide:

$$abla_{ heta} \mathbb{E}_{ au} \left[R
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Sum this formula over t, we obtain

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ight] \ &= \mathbb{E}\left[\sum_{t=0}^{T-1}
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Further reduce variance by introducing a baseline b(s)

$$abla_{ heta} \mathbb{E}_{ au} \left[R
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$$\nabla_{\theta} \mathbb{E}_{\tau} \left[R \right] = \mathbb{E}_{\tau} \left[\sum_{t=0}^{T-1} \nabla_{\theta} \log \pi(a_t \mid s_t, \theta) \left(\sum_{t'=t}^{T-1} r_{t'} - b(s_t) \right) \right]$$

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- Near optimal choice is expected return, $b(s_t) \approx \mathbb{E}\left[r_t + r_{t+1} + r_{t+2} + \cdots + r_{T-1}\right]$
- Interpretation: increase logprob of action a_t proportionally to how much returns $\sum_{t=t'}^{T-1} r_{t'}$ are better than expected

Discounts for Variance Reduction

Introduce discount factor γ , which ignores delayed effects between actions and rewards

$$abla_{ heta} \mathbb{E}_{ au} \left[R
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▶ Now, we want $b(s_t) \approx \mathbb{E}\left[r_t + \gamma r_{t+1} + \gamma^2 r_{t+2} + \dots + \gamma^{T-1-t} r_{T-1}\right]$

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- Write gradient estimator more generally as

$$egin{aligned}
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ight] \end{aligned}$$

 \hat{A}_t is the advantage estimate



"Vanilla" Policy Gradient Algorithm

```
Initialize policy parameter \theta, baseline b
for iteration=1, 2, \dots do
    Collect a set of trajectories by executing the current policy
    At each timestep in each trajectory, compute
      the return \hat{R}_t = \sum_{t'=t}^{T-1} \gamma^{t'-t} r_{t'}, and
     the advantage estimate \hat{A}_t = \hat{R}_t - b(s_t).
    Re-fit the baseline, by minimizing ||b(s_t) - R_t||^2.
      summed over all trajectories and timesteps.
    Update the policy, using a policy gradient estimate \hat{g},
      which is a sum of terms \nabla_{\theta} \log \pi(a_t \mid s_t, \theta) \hat{A}_t
end for
```

Advantage Actor-Critic

- Use neural network that represents policy π_{θ} and value function V_{θ} (approximating $V^{\pi_{\theta}}$)
- Pseudocode

for iteration=1, 2, . . . **do**
Agent acts for
$$T$$
 timesteps (e.g., $T=20$),
For each timestep t , compute
$$\hat{R}_t = r_t + \gamma r_{t+1} + \dots + \gamma^{T-t+1} r_{T-1} + \gamma^{T-t} V_{\theta}(s_t)$$

$$\hat{A}_t = \hat{R}_t - V_{\theta}(s_t)$$

 \hat{R}_t is target value function, in regression problem \hat{A}_t is estimated advantage function Compute loss gradient $g = \nabla_{\theta} \sum_{t=1}^{T} \left[-\log \pi_{\theta}(a_t \mid s_t) \hat{A}_t + c(V_{\theta}(s) - \hat{R}_t)^2 \right]$ g is plugged into a stochastic gradient ascent algorithm, e.g., Adam. end for

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- Makes use of a "surrogate objective" that estimates the performance of the policy around $\pi_{\rm old}$ used for sampling

$$L_{\pi_{\text{old}}}(\pi) = \frac{1}{N} \sum_{i=1}^{N} \frac{\pi(a_i \mid s_i)}{\pi_{\text{old}}(a_i \mid s_i)} \hat{A}_i$$
 (1)

Differentiating this objective gives the policy gradient

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Differentiating this objective gives the policy gradient

▶ $L_{\pi_{\text{old}}}(\pi)$ is only accurate when state distribution of π is close to π_{old} , thus it makes sense to constrain or penalize the distance $D_{\text{KL}}[\pi_{\text{old}} \parallel \pi]$



Pseudocode:

for iteration= $1, 2, \dots$ do

Run policy for T timesteps or N trajectories Estimate advantage function at all timesteps

$$\begin{array}{l} \operatorname{maximize} \sum_{n=1}^{N} \frac{\pi_{\theta}(a_{n} \mid s_{n})}{\pi_{\theta_{\mathrm{old}}}(a_{n} \mid s_{n})} \hat{A}_{n} \\ \text{subject to} & \overline{\mathrm{KL}}_{\pi_{\theta_{\mathrm{old}}}}(\pi_{\theta}) \leq \delta \end{array}$$

end for

- Can solve constrained optimization problem efficiently by using conjugate gradient
- Closely related to natural policy gradients (Kakade, 2002), natural actor critic (Peters and Schaal, 2005), REPS (Peters et al., 2010)



"Proximal" Policy Optimization

Use penalty instead of constraint

$$\underset{\theta}{\mathsf{maximize}} \sum_{n=1}^{N} \frac{\pi_{\theta}(a_n \mid s_n)}{\pi_{\theta_{\mathrm{old}}}(a_n \mid s_n)} \hat{A}_n - C \cdot \overline{\mathrm{KL}}_{\pi_{\theta_{\mathrm{old}}}}(\pi_{\theta})$$

► Pseudocode:

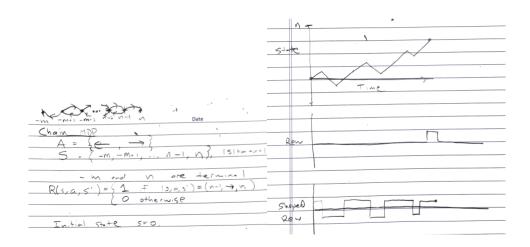
for iteration=1,2,... do Run policy for T timesteps or N trajectories Estimate advantage function at all timesteps Do SGD on above objective for some number of epochs If KL too high, increase β . If KL too low, decrease β .

end for

ightharpoonup pprox same performance as TRPO, but only first-order optimization



Variance Reduction for Policy Gradients



► Reward shaping: $\delta(s, a, s') = r(s, a, s') + \gamma \Phi(s') - \Phi(s)$ for arbitrary "potential" Φ

¹A. Y. Ng, D. Harada, and S. Russell. "Policy invariance under reward transformations: Theory and application: to reward shaping". «I@ML. 1999. » 🔾 🖎

- ► Reward shaping: $\delta(s, a, s') = r(s, a, s') + \gamma \Phi(s') \Phi(s)$ for arbitrary "potential" Φ
- ▶ Theorem: δ admits the same optimal policies as r.¹

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 - ▶ Proof sketch: suppose Q^* satisfies Bellman equation ($\mathcal{T}Q = Q$). If we transform $r \to \delta$, policy's value function satisfies $\tilde{Q}(s, a) = Q^*(s, a) \Phi(s)$

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- Theorem: δ admits the same optimal policies as R. A. Y. Ng, D. Harada, and S. Russell. "Policy invariance under reward transformations: Theory and application to reward shaping". ICML. 1999
- ▶ Alternative proof: advantage function is invariant. Let's look at effect on V^{π} and Q^{π} :

$$\mathbb{E} \left[\delta_{0} + \gamma \delta_{1} + \gamma^{2} \delta_{2} + \dots \right]$$

$$= \mathbb{E} \left[(r_{0} + \gamma \Phi(s_{1}) - \Phi(s_{0})) + \gamma (r_{1} + \gamma \Phi(s_{2}) - \Phi(s_{1})) + \gamma^{2} (r_{2} + \gamma \Phi(s_{3}) - \Phi(s_{2})) + \dots \right]$$

$$= \mathbb{E} \left[r_{0} + \gamma r_{1} + \gamma^{2} r_{2} + \dots - \Phi(s_{0}) \right]$$

Thus,

$$ilde{V}^\pi(s) = V^\pi(s) - \Phi(s) \ ilde{Q}^\pi(s) = Q^\pi(s,a) - \Phi(s) \ ilde{A}^\pi(s) = A^\pi(s,a)$$

$$A^{\pi}(s,\pi(s))=0$$
 at all states $\Rightarrow \pi$ is optimal



Reward Shaping and Problem Difficulty

• Shape with $\Phi = V^* \Rightarrow$ problem is solved in one step of value iteration

Reward Shaping and Problem Difficulty

- Shape with $\Phi = V^* \Rightarrow$ problem is solved in one step of value iteration
- Shaping leaves policy gradient invariant (and just adds baseline to estimator)

$$\begin{split} \mathbb{E} \big[\nabla_{\theta} \log \pi_{\theta}(a_{0} \mid s_{0})(r_{0} + \gamma \Phi(s_{1}) - \Phi(s_{0})) + \gamma(r_{1} + \gamma \Phi(s_{2}) - \Phi(s_{1})) \\ + \gamma^{2}(r_{2} + \gamma \Phi(s_{3}) - \Phi(s_{2})) + \dots \big] \\ = \mathbb{E} \left[\nabla_{\theta} \log \pi_{\theta}(a_{0} \mid s_{0})(r_{0} + \gamma r_{1} + \gamma^{2} r_{2} + \dots - \Phi(s_{0})) \right] \\ = \mathbb{E} \left[\nabla_{\theta} \log \pi_{\theta}(a_{0} \mid s_{0})(r_{0} + \gamma r_{1} + \gamma^{2} r_{2} + \dots) \right] \end{split}$$

Reward Shaping and Policy Gradients

▶ First note connection between shaped reward and advantage function:

$$\mathbb{E}_{s_1}[r_0 + \gamma V^{\pi}(s_1) - V^{\pi}(s_0) \mid s_0 = s, a_0 = a] = A^{\pi}(s, a)$$

Now considering the policy gradient and ignoring all but first shaped reward (i.e., pretend $\gamma=0$ after shaping) we get

$$egin{aligned} \mathbb{E}\left[\sum_{t}
abla_{ heta}\log\pi_{ heta}(a_{t}\mid s_{t})\delta_{t}
ight] &= \mathbb{E}\left[\sum_{t}
abla_{ heta}\log\pi_{ heta}(a_{t}\mid s_{t})(r_{t}+\gamma V^{\pi}(s_{t+1})-V^{\pi}(s_{t}))
ight] \ &= \mathbb{E}\left[\sum_{t}
abla_{ heta}\log\pi_{ heta}(a_{t}\mid s_{t})A^{\pi}(s_{t},a_{t})
ight] \end{aligned}$$

Reward Shaping and Policy Gradients

▶ Compromise: use more aggressive discount $\gamma\lambda$, with $\lambda \in (0,1)$: called generalized advantage estimation

$$\sum_{t} \nabla_{\theta} \log \pi_{\theta}(a_{t} \mid s_{t}) \sum_{k=0}^{\infty} (\gamma \lambda)^{k} \delta_{t+k}$$

Reward Shaping and Policy Gradients

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$$\sum_{t} \nabla_{\theta} \log \pi_{\theta}(a_{t} \mid s_{t}) \sum_{k=0}^{\infty} (\gamma \lambda)^{k} \delta_{t+k}$$

Or alternatively, use hard cutoff as in A3C

$$egin{aligned} \sum_t
abla_{ heta} \log \pi_{ heta}(a_t \mid s_t) \sum_{k=0}^{n-1} \gamma^k \delta_{t+k} \ &= \sum_t
abla_{ heta} \log \pi_{ heta}(a_t \mid s_t) \Biggl(\sum_{k=0}^{n-1} \gamma^k r_{t+k} + \gamma^n \Phi(s_{t+n}) - \Phi(s_t) \Biggr) \end{aligned}$$

Reward Shaping—Summary

► Reward shaping transformation leaves policy gradient and optimal policy invariant

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- Reward shaping transformation leaves policy gradient and optimal policy invariant
- lacktriangle Shaping with $\Phi pprox V^\pi$ makes consequences of actions more immediate

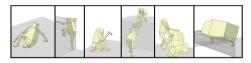
Reward Shaping—Summary

- ► Reward shaping transformation leaves policy gradient and optimal policy invariant
- Shaping with $\Phi \approx V^{\pi}$ makes consequences of actions more immediate
- ▶ Shaping, and then ignoring all but first term, gives policy gradient

Aside: Reward Shaping is Crucial in Practice

▶ I. Mordatch, E. Todorov, and Z. Popović. "Discovery of complex behaviors through contact-invariant optimization". *ACM Transactions on Graphics (TOG)* 31.4 (2012), p. 43

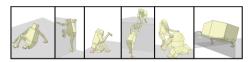
$$L\left(\mathbf{s}\right) = L_{\mathrm{CI}}\left(\mathbf{s}\right) + L_{\mathrm{Physics}}\left(\mathbf{s}\right) + L_{\mathrm{Task}}\left(\mathbf{s}\right) + L_{\mathrm{Hint}}\left(\mathbf{s}\right)$$



Aside: Reward Shaping is Crucial in Practice

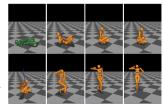
▶ I. Mordatch, E. Todorov, and Z. Popović. "Discovery of complex behaviors through contact-invariant optimization". *ACM Transactions on Graphics (TOG)* 31.4 (2012), p. 43

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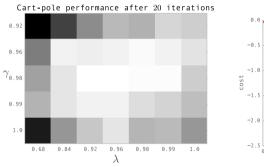
▶ Y. Tassa, T. Erez, and E. Todorov. "Synthesis and stabilization of complex behaviors through online trajectory optimization". *Intelligent Robots and Systems (IROS), 2012 IEEE/RSJ International Conference on.* IEEE. 2012, pp. 4906–4913

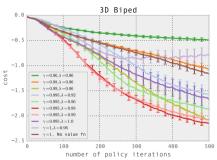
The state-cost is composed of 4 terms. The first term penalizes the horizontal distance (in the xy-plane) between the center-of-mass (CoM) and the mean of the feet positions. The second term penalizes the horizontal distance between the torso and the CoM. The third penalizes the vertical distance between the torso and a point 1.3m over the mean of the feet. All three terms use the semonth-abs norm (Figure 2).



Choosing parameters γ, λ

Performance as γ, λ are varied



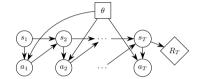


(Generalized Advantage Estimation for Policy Gradients, S. et al., ICLR 2016)

Pathwise Derivative Methods

Deriving the Policy Gradient, Reparameterized

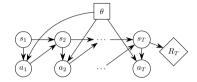
► Episodic MDP:



Want to compute $\nabla_{\theta} \mathbb{E}[R_T]$. We'll use $\nabla_{\theta} \log \pi(a_t \mid s_t; \theta)$

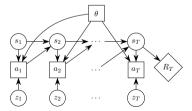
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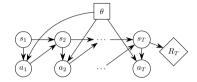
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▶ Reparameterize: $a_t = \pi(s_t, z_t; \theta)$. z_t is noise from fixed distribution.



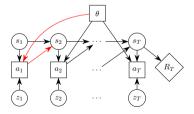
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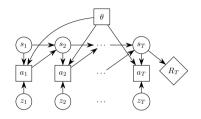
▶ Reparameterize: $a_t = \pi(s_t, z_t; \theta)$. z_t is noise from fixed distribution.



▶ Only works if $P(s_2 | s_1, a_1)$ is known $\ddot{-}$



Using a *Q*-function

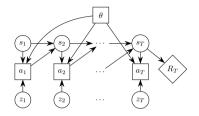


$$\frac{\mathrm{d}}{\mathrm{d}\theta} \mathbb{E}\left[R_{T}\right] = \mathbb{E}\left[\sum_{t=1}^{T} \frac{\mathrm{d}R_{T}}{\mathrm{d}a_{t}} \frac{\mathrm{d}a_{t}}{\mathrm{d}\theta}\right] = \mathbb{E}\left[\sum_{t=1}^{T} \frac{\mathrm{d}}{\mathrm{d}a_{t}} \mathbb{E}\left[R_{T} \mid a_{t}\right] \frac{\mathrm{d}a_{t}}{\mathrm{d}\theta}\right]$$
$$= \mathbb{E}\left[\sum_{t=1}^{T} \frac{\mathrm{d}Q(s_{t}, a_{t})}{\mathrm{d}a_{t}} \frac{\mathrm{d}a_{t}}{\mathrm{d}\theta}\right] = \mathbb{E}\left[\sum_{t=1}^{T} \frac{\mathrm{d}}{\mathrm{d}\theta}Q(s_{t}, \pi(s_{t}, z_{t}; \theta))\right]$$

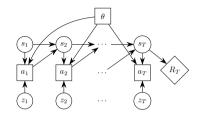
▶ Learn Q_{ϕ} to approximate $Q^{\pi,\gamma}$, and use it to compute gradient estimates.

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- Pseudocode:

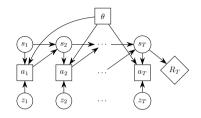
```
for iteration=1,2,... do 
Execute policy \pi_{\theta} to collect T timesteps of data 
Update \pi_{\theta} using g \propto \nabla_{\theta} \sum_{t=1}^{T} Q(s_t, \pi(s_t, z_t; \theta)) 
Update Q_{\phi} using g \propto \nabla_{\phi} \sum_{t=1}^{T} (Q_{\phi}(s_t, a_t) - \hat{Q}_t)^2, e.g. with \mathsf{TD}(\lambda) end for
```



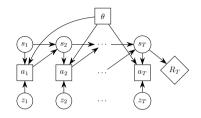
▶ Instead of learning Q, we learn



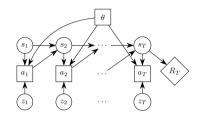
- ▶ Instead of learning Q, we learn
 - State-value function $V pprox V^{\pi,\gamma}$



- ightharpoonup Instead of learning Q, we learn
 - State-value function $V \approx V^{\pi,\gamma}$
 - ▶ Dynamics model f, approximating $s_{t+1} = f(s_t, a_t) + \zeta_t$



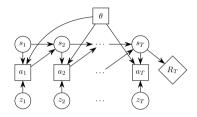
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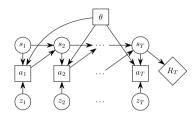


$SVG(\infty)$ Algorithm



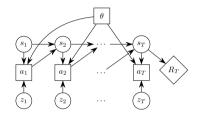
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$SVG(\infty)$ Algorithm



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$SVG(\infty)$ Algorithm



- ▶ Just learn dynamics model *f*
- Given whole trajectory, infer all noise variables
- ► Freeze all policy and dynamics noise, differentiate through entire deterministic computation graph

SVG Results

Applied to 2D robotics tasks

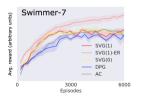


SVG Results

Applied to 2D robotics tasks



▶ Overall: different gradient estimators behave similarly





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- Problem: there's no exploration.
- ► Solution: add noise to the policy, but estimate *Q* with TD(0), so it's valid off-policy
- Policy gradient is a little biased (even with $Q=Q^{\pi}$), but only because state distribution is off—it gets the right gradient at every state

- Incorporate replay buffer and target network ideas from DQN for increased stability
- ▶ Use lagged (Polyak-averaging) version of Q_{ϕ} and π_{θ} for fitting Q_{ϕ} (towards $Q^{\pi,\gamma}$) with TD(0)

$$\hat{Q}_t = r_t + \gamma Q_{\phi'}(s_{t+1}, \pi(s_{t+1}; \theta'))$$

Pseudocode:

```
for iteration=1,2,... do Act for several timesteps, add data to replay buffer Sample minibatch Update \pi_{\theta} using g \propto \nabla_{\theta} \sum_{t=1}^{T} Q(s_t, \pi(s_t, z_t; \theta)) Update Q_{\phi} using g \propto \nabla_{\phi} \sum_{t=1}^{T} (Q_{\phi}(s_t, a_t) - \hat{Q}_t)^2, end for
```

DDPG Results

Applied to 2D and 3D robotics tasks and driving with pixel input



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 - SVG(1): $\frac{d}{ds}(r + \gamma V(s'))$ (learn f, V)

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 - ► SVG(∞): $\frac{\mathrm{d}}{\mathrm{d}a_t}(r_t + \gamma r_{t+1} + \gamma^2 r_{t+2} + \dots)$ (learn f)

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- Pathwise derivative methods more sample-efficient when they work (maybe), but work less generally due to high bias

Thanks

Questions?